

Comp 411
Principles of Programming Languages
Lecture 14
Eliminating Lambda Using Combinators

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OO Code Samples

- Show selections from solution to Assignment 2
 - Class hierarchy for Binding union
 - Sample visitor method code
- Discuss some OO design tradeoffs
 - Use of **instanceof**
 - With composite, visitor implementation of methods is not always mandated. Good idea to “build in” some core operations of a composite using the interpreter pattern. Why? Leaner (in terms of lines of code). Easier to read.

Good Commenting Conventions

- Javadoc description for every class, field, non-trivial method.
- Method descriptions are informal contracts. Contracts should be as precise as possible. In some cases (e.g., GUI libraries), complete precision may not be feasible.
- Sample solutions could be better commented.

How to Eliminate **lambda**

Goal: devise a few combinators (functions expressed in lambda-notation with no free variables) that enable us to express all λ -expressions without explicitly using λ .

Notation: let $\lambda^* x.M$ denote $\lambda x.M$ converted to a form that eliminates the starred λ . Then

- $\lambda^* x.x \rightarrow \mathbf{I}$ (where $\mathbf{I} = \lambda x.x$)
- $\lambda^* x.y \rightarrow \mathbf{K} y$ (where $\mathbf{K} = \lambda y.\lambda x.y$)
- $\lambda^* x.M N \rightarrow \mathbf{S} (\lambda^* x.M) (\lambda^* x.N)$
(where $\mathbf{S} = \lambda x.\lambda y.\lambda z. (y x) (z x)$)

Strategy: eliminate λ -abstractions from inside out, one-at-a-time. Any order works. Transformation can cause exponential blow-up.

Note: \mathbf{I} is technically unnecessary since $\mathbf{SKK} = \mathbf{I}$