



Crypto Protocols, part 2

Today's talk includes slides from:
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Example - Needham-Schroeder

- The Needham- Schroeder symmetric-key protocol [NS78]

A → S: A, B, Na

S → A: {Na, B, Kc, {Kc, A}Kb }Ka

A → B: {Kc, A}Kb

B → A: {Nb}Kc

A → B: {Nb-1}Kc

- A, B are "principals;" S is a trusted key server
- Ka, Kb are secret keys shared with S
- {X, Y}K means: X concatenated with Y, encrypted with K
- Na, Nb are "nonces;" fresh (not used before)
- Kc is a fresh connection key

Denning-Sacco Attack

- Assumes that the attacker has recorded a previous session, and compromised the connection key K_x used in that one.
 - $A \rightarrow B: \{K_x, A\}_{K_b}$ *attacker replayed old message*
 - $B \rightarrow A: \{N_b\}_{K_x}$
 - $A \rightarrow B: \{N_{b-1}\}_{K_x}$ *forged by attacker*
- B now believes he shares a fresh secret key K_x with A.
- Denning-Sacco moral: use a timestamp (calendar clock value) to detect replay of old messages.

Belief Logic

- Burrows, Abadi, and Needham (BAN) Logic [BAN90a]
 - Modal logic of belief ("belief" as local knowledge)
 - Special constructs and inference rules
 - e.g., $P \text{ sees } X$ (P has received X in a message)
 - Protocol messages are "idealized" into logical statements
 - Objective is to prove that both parties share common beliefs

Constructs

P bel X	P believes X
P sees X	P received X in a message
P said X	P once said X
P controls X	P has jurisdiction over X
fresh(X)	X has not been used before
P \leftarrow -K- \rightarrow Q	P and Q may use key K for private communication
K- \rightarrow P	P has K as public key
P \leftarrow -X- \rightarrow Q	X is a secret shared by P and Q
{X}K	X encrypted under K
\langle X \rangle Y	X combined with Y
K ⁻¹	inverse key to K

(This symbolism is not quite standard)

BAN Inference Rules

- These inferences are supposed to be valid despite attacker interference.

(1) Message-meaning rules

$P \text{ bel } Q \leftarrow K \rightarrow P, P \text{ sees } \{X\}K \quad |- \quad P \text{ bel } Q \text{ said } X$
 $P \text{ bel } K \rightarrow Q, P \text{ sees } \{X\}K^{-1} \quad |- \quad P \text{ bel } Q \text{ said } X$
 $P \text{ bel } Q \leftarrow Y \rightarrow P, P \text{ sees } \langle X \rangle Y \quad |- \quad P \text{ bel } Q \text{ said } X$

(2) Nonce-verification

$P \text{ bel fresh}(X), P \text{ bel } Q \text{ said } X \quad |- \quad P \text{ bel } Q \text{ bel } X$

(3) Jurisdiction

$P \text{ bel } Q \text{ controls } X, P \text{ bel } Q \text{ bel } X \quad |- \quad P \text{ bel } X$

More BAN Rules

(4) Sees rules

$P \text{ sees } (X, Y) \quad |- \quad P \text{ sees } X, P \text{ sees } Y$

$P \text{ sees } \langle X \rangle Y \quad |- \quad P \text{ sees } X$

$P \text{ bel } Q \leftarrow K \rightarrow P, P \text{ sees } \{X\}K \quad |- \quad P \text{ sees } X$

$P \text{ bel } K \rightarrow P, P \text{ sees } \{X\}K \quad |- \quad P \text{ sees } X$

$P \text{ bel } K \rightarrow Q, P \text{ sees } \{X\}K^{-1} \quad |- \quad P \text{ sees } X$

(5) Freshness

$P \text{ bel fresh}(X) \quad |- \quad P \text{ bel fresh}(X, Y) \text{ (inside encryption)}$

- Symmetry of $\leftarrow K \rightarrow$ and $\leftarrow X \rightarrow$ is implicitly used
- Conjunction is handled implicitly

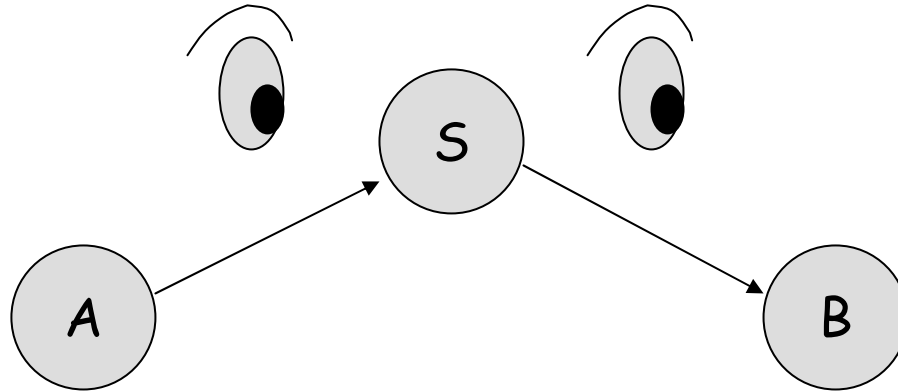
$P \text{ bel } (X, Y) \quad |- \quad P \text{ bel } X \text{ and } P \text{ bel } Y$

$P \text{ bel } Q \text{ said } (X, Y) \quad |- \quad P \text{ bel } Q \text{ said } X, P \text{ bel } Q \text{ said } Y$

Protocol Idealization

- Convert a protocol into a collection of statements
 - Assumptions
 - Message idealizations
 - Security goals
- Message idealization conveys intent of message
 - Example: $A \rightarrow B: \{A, K_{ab}\}_{K_{bs}}$
 - Idealized: $B \text{ sees } \{A \leftarrow K_{ab} \rightarrow B\}_{K_{bs}}$
- *Note: only encrypted fields are retained in the idealization.*

Example - Wide-Mouthed Frog



$A \rightarrow S: A, \{T, B, K_{ab}\}_{K_{as}} \rightarrow (M1) S \text{ sees } \{T, A \leftarrow K_{ab} \rightarrow B\}_{K_{as}}$
 $S \rightarrow B: \{T, A, K_{ab}\}_{K_{bs}} \rightarrow (M2) B \text{ sees } \{T, A \text{ bel } A \leftarrow K_{ab} \rightarrow B\}_{K_{bs}}$

- (A1) $P \text{ bel fresh}(T)$, for $P = A, B, S$
- (A2) $B \text{ bel } A \text{ controls } A \leftarrow K_{ab} \rightarrow B$
- (A3) $S \text{ bel } A \leftarrow K_{as} \rightarrow S$, $B \text{ bel } B \leftarrow K_{bs} \rightarrow S$
- (A4) $B \text{ bel } S \text{ controls } A \text{ bel } A \leftarrow K_{ab} \rightarrow B$
- (A5) $A \text{ bel } A \leftarrow K_{ab} \rightarrow B$

T is a timestamp
 A generates K_{ab}
 K_{as} , K_{bs} are shared with S
 S should check this
Justifies A said $A \leftarrow K_{ab} \rightarrow B$

Analysis

- Goal: prove that $B \text{ bel } A \leftarrow\text{-Kab-}\rightarrow B$.

- Proof:

$B \text{ sees } \{T, A \text{ bel } A \leftarrow\text{-Kab-}\rightarrow B\}Kbs$	M2
$B \text{ bel } S \text{ said } (T, A \text{ bel } A \leftarrow\text{-Kab-}\rightarrow B)$	A3, rule 1
$B \text{ bel fresh}(T, A \text{ bel } A \leftarrow\text{-Kab-}\rightarrow B)$	A1, rule 5
$B \text{ bel } S \text{ bel } (T, A \text{ bel } A \leftarrow\text{-Kab-}\rightarrow B)$	rule 2
$B \text{ bel } S \text{ bel } A \text{ bel } A \leftarrow\text{-Kab-}\rightarrow B$	conjunction
$B \text{ bel } A \text{ bel } A \leftarrow\text{-Kab-}\rightarrow B$	A4, rule 3
$B \text{ bel } A \leftarrow\text{-Kab-}\rightarrow B$	A2, Rule 3

- Exercises:

- Prove that $S \text{ bel } A \text{ bel } A \leftarrow\text{-Kab-}\rightarrow B$
- Add the message $B \rightarrow A: \{T\}Kab$ (M3) and show that $A \text{ bel } B \text{ bel } A \leftarrow\text{-Kab-}\rightarrow B$

Nessett's Critique

- Awkward example in [Nes90]

$A \rightarrow B: \{T, K_{ab}\}K_a^{-1} \dashrightarrow B \text{ sees } \{T, A \leftarrow K_{ab} \rightarrow B\}K_a^{-1}$

- Assumptions

(A1) $B \text{ bel } K_a \rightarrow A$

(A2) $A \text{ bel } A \leftarrow K_{ab} \rightarrow B$

(A3) $B \text{ bel fresh}(T)$

(A4) $B \text{ bel } A \text{ controls } A \leftarrow K_{ab} \rightarrow B$

- Goal: $B \text{ bel } A \leftarrow K_{ab} \rightarrow B$

- Proof:

$B \text{ bel } A \text{ said } (T, A \leftarrow K_{ab} \rightarrow B)$ A1, rule 1

$B \text{ bel fresh}(T, A \leftarrow K_{ab} \rightarrow B)$ A3, rule 5

$B \text{ bel } A \text{ bel } (T, A \leftarrow K_{ab} \rightarrow B)$ rule 2

$B \text{ bel } A \leftarrow K_{ab} \rightarrow B$ A4, rule 3

- *Problem: K_a is a public key, so K_{ab} is exposed.*

Observations

- According to "Rejoinder" [BAN90b], "There is no attempt to deal with ... unauthorized release of secrets"
- The logic is monotonic: if a key is believed to be good, the belief cannot be retracted
- The protocol may be inconsistent with beliefs about confidentiality of keys and other secrets
- More generally - one should analyze the protocol for consistency with its idealization
- Alternatively - devise restrictions on protocols and idealization rules that guarantee consistency

Subsequent Developments

- Discussions and semantics, e.g., [Syv91]
- More extensive logics, e.g., GNY (Gong-Needham-Yahalom) [GNY90] and SVO [SvO94]
- GNY extensions:
 - Unencrypted fields retained
 - "P possesses X" construct and possession rules
 - "not originated here" operator
 - Rationality rule: if $X \vdash Y$ then $P \text{ bel } X \vdash P \text{ bel } Y$
 - "message extension" links fields to assertions
- Mechanization of inference, e.g., [KW96, Bra96]
 - User still does idealization
- Protocol vs. idealization problem still unsolved

Model-Checking

- Application of software tools designed for hardware CAD
 - Verification by state space exploration - exhaustive on model
- Like earlier Prolog tool approach, but
 - Forward search rather than reverse search
 - Special algorithms (BDDs, etc.)
 - A priori finite model (no unbounded recursion)
 - Fully automatic once protocol is encoded
- Practicioners:
 - Roscoe [Ros95], using FDR (the first)
 - Mitchell, et al, using Murphi [MMS97]
 - Marrero, et al, using SMV [MCJ97]
 - Denker, et al, using Maude [DMT98]
 - ... and more

Model-Checking Observations

- *Very effective* at finding flaws, but
- No guarantee of correctness, due to artificial finite bounds
- Setup and analysis is quick when done by experts
- Automatic translation from simple message-list format to model-checker input is possible [Low98a, Mil97]
- “Killer” example: Lowe attack on Needham-Schroeder public-key protocol, using FDR [Low96]

NSPK Protocol

- N_a, N_b are nonces; PK_A, PK_B are public keys
- The protocol - final handshake
 - $A \rightarrow B: \{N_a, A\}_{PK_B}$
 - $B \rightarrow A: \{N_a, N_b\}_{PK_A}$
 - $A \rightarrow B: \{N_b\}_{PK_B}$
- Exercise: use BAN Logic to prove
 $B \text{ bel } A \text{ bel } A \leftarrow N_b \rightarrow B$ [BAN90a]

Lowé Attack on NSPK

- X is the attacker acting as a principal
- X masquerades as A for B

Session 1: A to X

A → X: {Na, A}PKX

X → A: {Na, Nb}PKA

A → X: {Nb}PKX

Session 2: X (as A) to B

A(X) → B: {Na, A}PKB

B → A(X): {Na, Nb}PKA

A(X) → B: {Nb}PKB

(Lowé's modification to fix it: B → A: {Na, Nb, B}PKA)

Finiteness Limitation

- How many sessions must be simulated to ensure coverage?
 - Lowe attack needed two sessions
 - Example 1.3 in Dolev-Yao [DY83] needed three sessions
 - $A \rightarrow B: \{\{M\}_{PK_b}, A\}_{PK_b}$
 - $B \rightarrow A: \{\{M\}_{PK_a}, B\}_{PK_a}$
- No algorithmically determined bound is possible for all cases
 - Because of undecidability for the model
- Possible bounds for limited classes of protocols
 - Lowe "small system" result [Low98b]: one honest agent per role, one time, if certain restrictions are satisfied:
 - Encrypted fields are distinguishable
 - Principal identities in every encrypted field
 - No temporary secrets
 - No forwarding of encrypted fields

Inductive Proofs

- Approach: like proofs of program correctness
 - Induction to prove "loop invariant"
- State-transition model, objective is security invariant
- General-purpose specification/verification system support
 - Kemmerer, using Ina Jo and ITP [Kem89] (the first)
 - Paulson, using Isabelle [Paul98] (the new wave)
 - Dutertre and Schneider, using PVS [DS97]
 - Bolignano, using Coq [Bol97]
- Can also be done manually [Sch98, THG98]
 - Contributed to better understanding of invariants
 - Much more complex than belief logic proofs
- Full guarantee of correctness (with respect to model)
 - Proofs include confidentiality

Summary

- Cryptographic protocol verification is based on models where
 - Encryption is perfect (strong encryption)
 - The attacker intercepts all messages (strong attacker)
 - Security is undecidable in general, primarily because the number of sessions is unbounded.
- Belief logic analysis:
 - Requires "idealization" of the protocol
 - Does not address confidentiality
 - Can be performed easily, manually or with automated support
- State-exploration approaches
 - Use model-checking tools
 - Are effective for finding flaws automatically
 - Are limited by finiteness

Summary, cont'd

- Inductive proofs
 - Can prove correctness
 - Require substantial effort
 - Can be done manually, but preferably with verification tools
- Protocol security verification is still a research area
 - But experts can do it fairly routinely
- "Real" protocols are difficult to analyze for practical reasons
 - Specifications are not precise
 - They use operators with more complex properties than simple abstract encryption
 - Flow of control is more complex - protocols negotiate alternative encryption algorithms and other parameters
 - Messages have many fields not relevant to provable security