

Comp 411
Principles of Programming Languages
Lecture 13
Eliminating Lambda Using Combinators

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How to Eliminate λ

Goal: devise a few combinators (functions expressed in lambda-notation with no free variables) that enable us to express all λ -expressions without explicitly using λ .

Notation: let $\lambda^* x.M$ denote $\lambda x.M$ converted to a form that eliminates the starred λ . Then

- $\lambda^* x.x \rightarrow I$ (where $I = \lambda x.x$)
- $\lambda^* x.y \rightarrow K y$ (where $K = \lambda y.\lambda x.y$)
- $\lambda^* x.(M N) \rightarrow S (\lambda^* x.M) (\lambda^* x.N)$
(where $S = \lambda x.\lambda y.\lambda z.(x z)(y z)$)

Strategy: eliminate λ -abstractions from inside out, one-at-a time. Any order works. Transformation can cause exponential blow-up. (Try converting Y .)

Note: I is technically unnecessary since $SKK = I$