

How to design an HMM for a new problem

- Architecture/topology design:
 - What are the states, observation symbols, and the topology of the state transition graph?
- Learning/Training:
 - Fully annotated or partially annotated training datasets
 - Parameter estimation by maximum likelihood or by EM
- Validation/Testing:
 - Fully annotated testing datasets
 - Performance evaluation (accuracy, specificity and sensitivity)

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HMM model structure

Duration modeling



What is the probability of staying with the fair coin for T time steps?

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Inherent limitation of HMMs

 The duration in state F follows an exponentially decaying distribution called a geometric distribution.

$$P(X = F^T) = (0.95)^{T-1}(0.05)$$

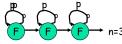
 The geometric distribution gives too much probability to short sequences of Fs and Ls and too little to medium and long sequences of Fs and Ls.

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Duration modeling

 To obtain non-geometric length distributions, we use an array of n F states, as follows:



$$P(|X|=L) = {\binom{L-1}{n-1}} p^{L-n} (1-p)^n$$

 Generated length distribution is a negative binomial.

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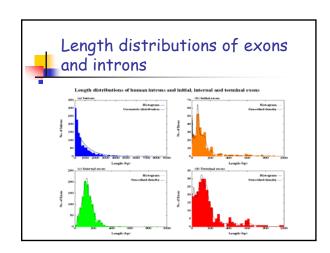
Why does this matter?

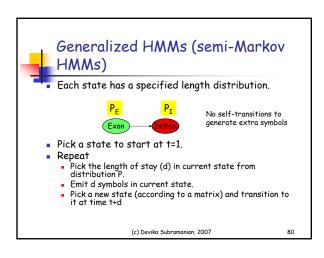


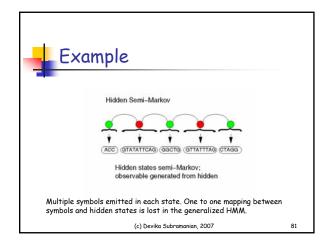
- Length of stay in "Exon" state determines length of predicted exons. Very short exons are rare.
- Similarly for introns. Introns shorter than 30 bp do not exist.

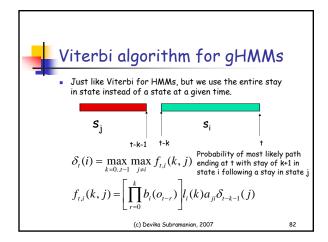
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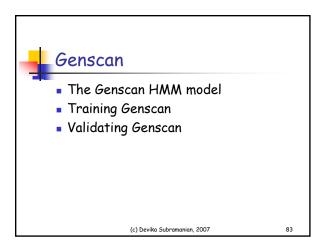
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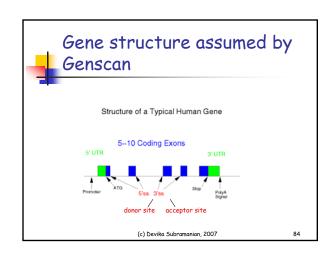


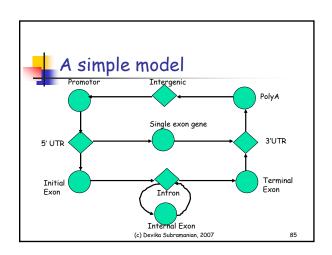


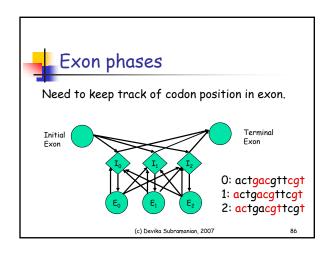










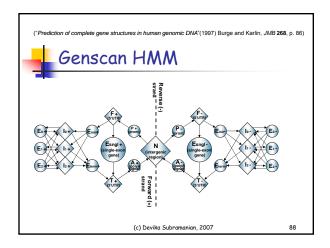




Genscan's architecture (1)

- HMM states for exons and introns in three different phases, single exon, 5' and 3' UTRs, promoter region, polyA site and intergenic region.
- Explicit length modeling of introns and exons.

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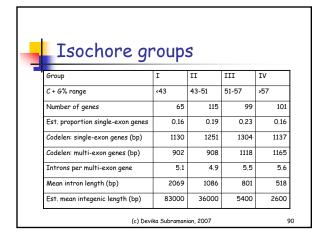


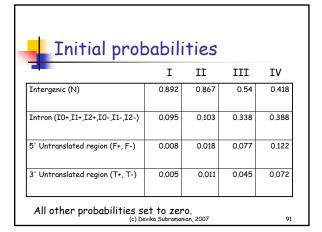


Genscan model components

- Vector of initial probabilities: π
- State Transition probability Matrix: a
- Set of length distributions: f_q conditional on state q.
- Emission probabilities: P(s|q,d) conditional on state and length.

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Transition probabilities

- Probabilities of state transitions not present in model are zero.
- Deterministic transitions are assigned probability 1.
- The others transition probabilities are set according to maximum likelihood values in training data.

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Length distribution for introns

- No introns < 65bp. After that geometric (exponential) distribution.
- Substantial difference between different C+G groups.
- So, intron length is modeled as geometric distribution with different parameters of different C+G groups.

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Exon length distribution model

- Exons are very important to model.
- Substantial differences in length distribution between initial, internal and terminal exons.
- No substantial difference between different C+G compositional groups.
- Exon length means considered between 50 and 300 bps.
- Account for phase (3*codons + phase)

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Other length distributions

- 5' UTR -> Geometric with mean 769bp
- 3' UTR -> Geometric with mean 457bp

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Emission models

- Exons -- inhomogeneous 3-periodic 5th order Markov model.
- Introns and intergenic regions homogeneous 5th order Markov model
- 5' and 3' UTRs homogeneous 5th order Markov model

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Emission models for exons and introns

5th order inhomogeneous Markov model



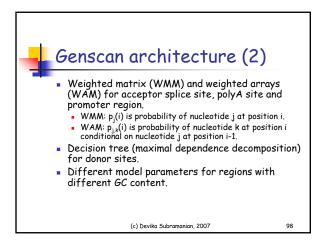
In an *inhomogeneous* Markov model, we have different distributions at different positions in the sequence.

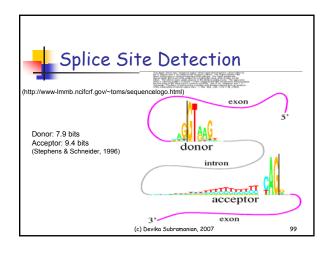
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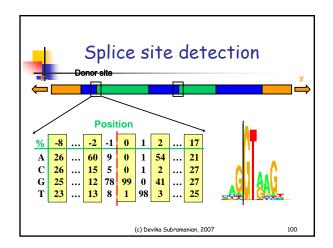
5th order homogeneous Markov model :

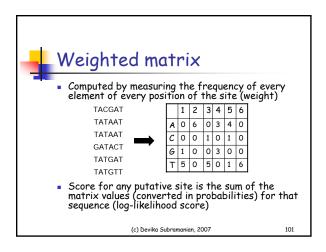
 $P(o_t | o_{t-1}o_{t-2}o_{t-3}o_{t-4}o_{t-5})$

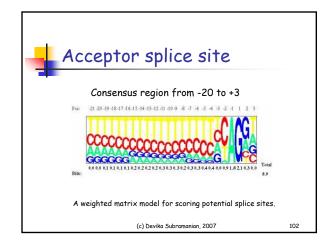
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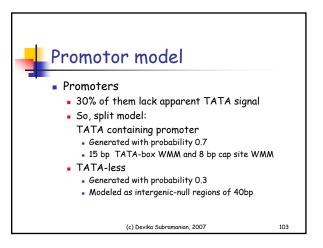










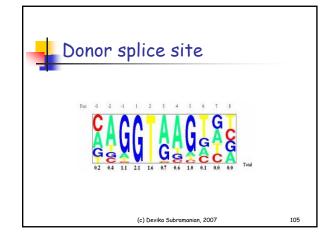




Transcriptional and Translational Signals

- PolyA signal
 - 6 base pairs WMM (AATAAA)
- Translation Initiation signal
 - 12 base pairs WMM (6 base pairs prior to start codon)
- Translation termination signal
 - 1 of 3 stop codons according to observed frequency
 - Next 3 nucleotides using WMM

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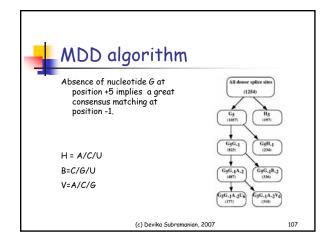


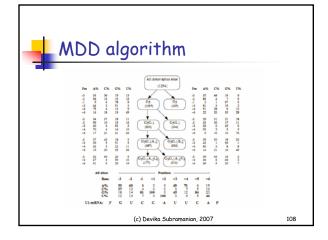
Donor splice site model

- Consensus region -3 to +6 (3 on exon, 6 on intron)
- WMM or WAM not sufficient to model because of dependencies on non-adjacent nucleotides.

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Using Genscan for gene finding

- Model's goal is to generate "Optimal Parse"
- Parse (X) consists of
 - Ordered set of states = $\{s_1, s_2, ..., s_n\}$ where $s_i \in \{S_j / j=1 \text{ to 27}\}$
 - Associated lengths (durations)
 (d) = {d₁,d₂,...,d_n}
 - It generates DNA sequence O of length $L = \sum_{i=1 \text{ to } n} d_i$.

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Running the model

- An initial state s_1 is chosen according to an initial distribution π on the states, i.e. $\pi_i = P(s_i = S_i)$
- A length distribution d₁ is generated conditional on s_{1,i.e.} f_{s1} (d₁)
- A sequence segment s_1 of length d_1 is generated conditional of s_1 and d_1 i.e. $P(s_i|s_1,d_1)$
- Subsequent state s_2 is generated, conditional on s_1 . First order Markov. $a_{ij} = P(s_{k+1} = S_j \mid s_k = S_i)$

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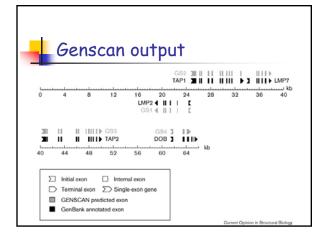


Using model

 Optimal parse can be computed by Viterbi algorithm for generalized HMMs (see Rabiner's extension in section 4D, pages 269-270).

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Genscan

- The Genscan HMM model
- Training Genscan
- Validating Genscan

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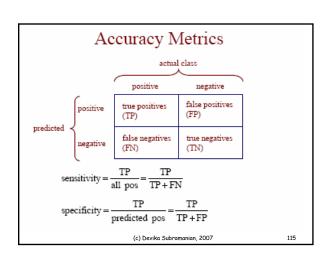
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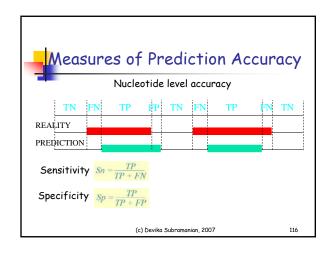


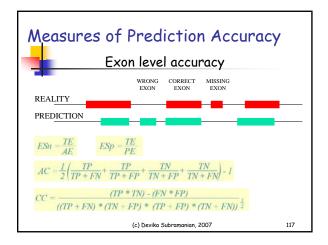
Evaluating gene finders

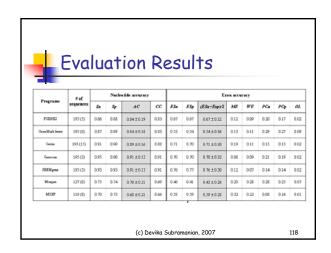
- Calculating accuracy of programs' predictions
- Several evaluation studies:
 - Burset and Guigó, 1996 (vertebrate sequences)
 - Pavy et al., 1999 (Arabidopsis thaliana)
 - Rogic et al., 2001 (mammalian sequences)

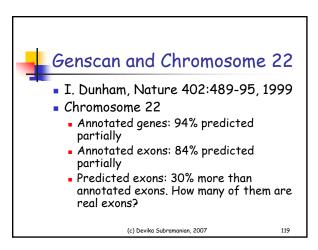
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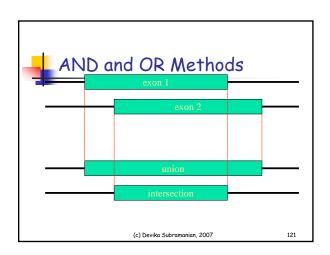


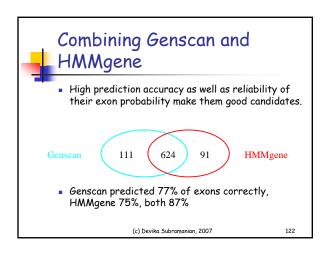


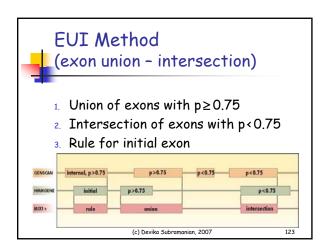


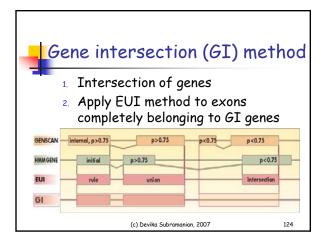


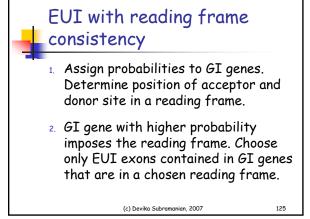
- Programs that integrate results of similarity searches with ab initio techniques (GenomeScan, FGENESH+, Procrustes)
- Programs that use synteny between organisms (ROSETTA, SLAM)
- Integration of programs predicting different elements of a gene (EuGène)
- Combining predictions from several gene finding programs (combination of experts)
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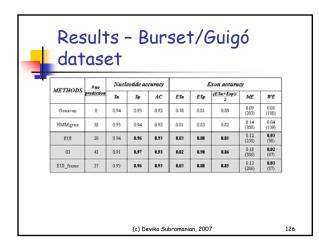














Summary: Eukaryotic gene finding

- Overall accuracy usually below 50%
 - Human gene finding is hardest
 - Very long introns, and lots of them
- Leading methods: HMMs and variants
- New ideas needed
- New opportunity: use sequence of related species

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