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# Workload Characterization

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# Goals for Today

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## Understand

- Different approaches for characterizing workload

# Workload Characterization

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## Two key parts

- Observe key performance characteristics of a workload
- Develop a model that can be used for further study
- Terms
  - workload unit/component: present service requests to SUT interface
    - examples: each application in a set, sites, user sessions
    - components should be homogeneous if possible, otherwise split
- Workload parameters:
  - measured quantities that depend on workload not system
  - types
    - service requests
    - resource demands
  - examples
    - transaction types, instructions, packet types & destinations
    - page reference patterns

# Techniques for Workload Characterization

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- Averaging
- Specifying Dispersion
- Single-parameter histograms
- Multiparameter histograms
- Principal components analysis
- Markov models
- Clustering

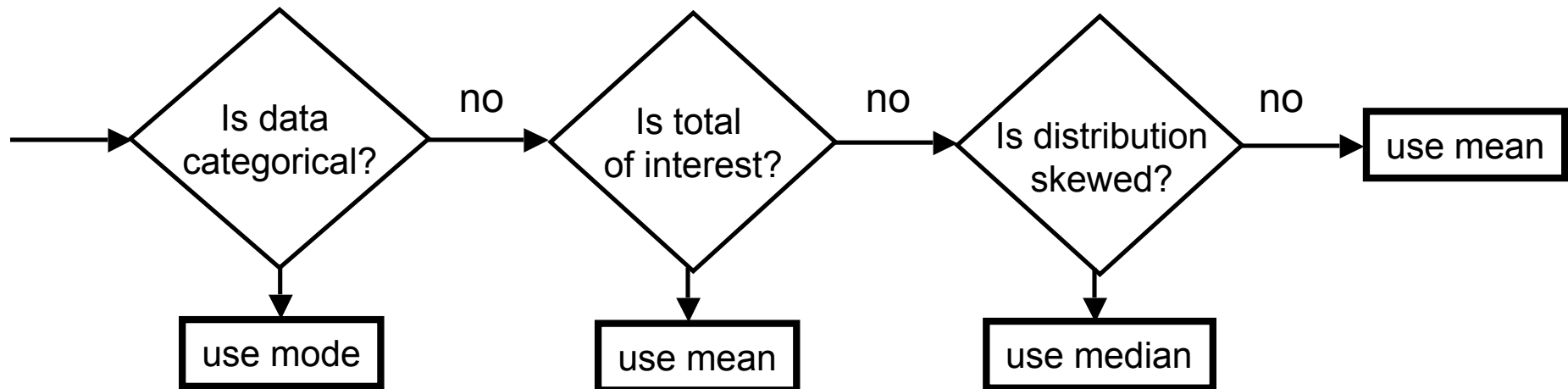
Note: the items marked in red will be discussed in the next lecture

# Averaging

aka arithmetic mean of values  $\{x_1, x_2, \dots, x_n\}$

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

- **Caution:** arithmetic mean is not always appropriate “index of central tendency”



- Median = 50th percentile value
- Mode = most frequent
  - e.g. most frequent destination for packets

# Specifying Dispersion

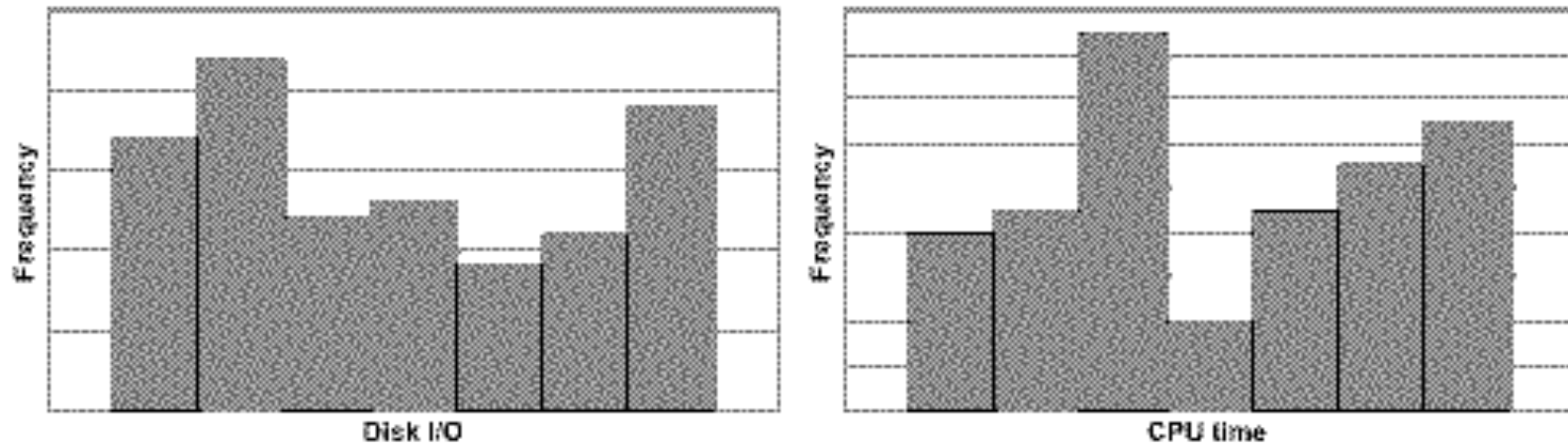
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- Averaging is insufficient if  $\exists$  large variability in data values
- Variability of  $\{x_1, x_2, \dots, x_n\}$  is commonly specified by **variance**

sample variance 
$$s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$$

- **Sample standard deviation**,  $s = \text{sqrt}(\text{sample variance})$ 
  - often more meaningful: same units as the mean
- **Alternatives for summarizing variability**
  - range: maximum - minimum
  - 10 and 90 percentiles
  - semi-interquartile range (SIQR) =  $(x_{[.75(n-1)+1]} - x_{[.25(n-1)+1]})/2$
  - mean absolute deviation =  $\frac{1}{n} \sum_{i=1}^n |x_i - \bar{x}|$
- **Coefficient of variation** = ratio of std. dev to mean =  $s/\bar{x}$ 
  - if C.O.V. = 0,  $\forall_i x_i = c$ ; high C.O.V.  $\Rightarrow$  mean is not sufficient

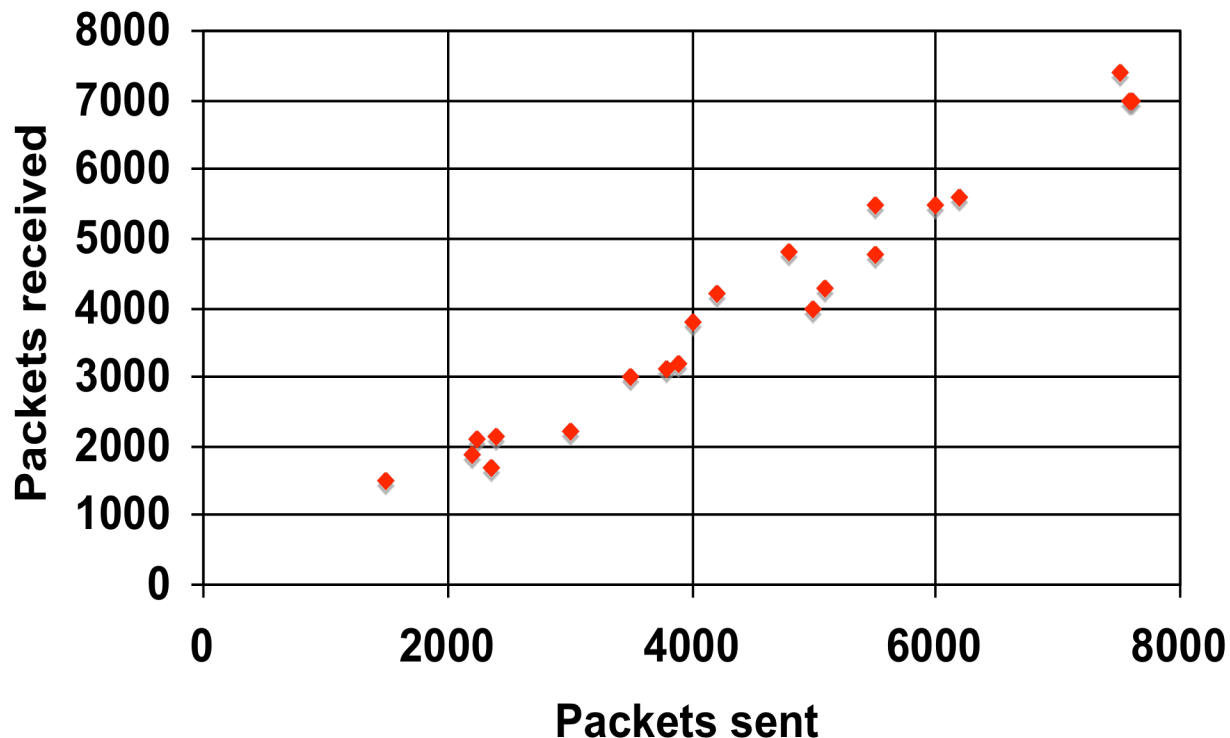
# Single-parameter Histograms



- **SPH: relative frequencies of various values of a parameter**
  - divide complete range into buckets
  - count observations that fall in each
- **Uses**
  - simulation: generate test workload matching distribution
  - analytical model: validate probability distribution used in model
- **Disadvantages**
  - much data:  $n$  buckets,  $m$  parameters/ component,  $k$  components
    - should only be used if variance is high and averages are inappropriate
  - SPH ignore correlation among parameters

# Multiparameter Histograms

- MPH: use when significant correlation between parameters



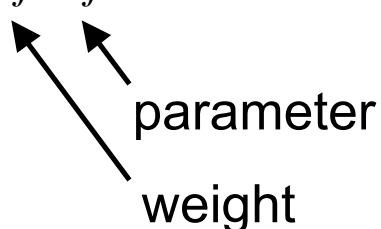
- Disadvantages
  - rendering more than 2-parameter histograms is problematic
  - much detail; uncommon to use them



# Weighted Sum of Parameters

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- **Classify workload components by weighted sum of their parameter values**

$$y = \sum_{j=1}^n a_j x_j$$


parameter

weight

- **Use  $y$  to classify components into categories, e.g. high, low**
- **Problem: choosing appropriate weights for parameters**  
—bad choice of weights may group dissimilar components

# Principal-Component Analysis

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## Choosing Good Weights

- **Problem**
  - find weights so that weighted sums provide maximum discrimination among components

$$y_i = \sum_{j=1}^n a_{ij} x_j$$

- **For each component i,**
  - $y_i$  is a linear combination of parameter values  $x_j$
  - $a_{ij}$  is loading of  $x_j$  on  $y_i$
- **Choose weights so that y's form an orthogonal set, namely**

$$\langle y_i, y_j \rangle = \sum_k a_{ik} a_{kj} = 0$$

- **Properties: y's form an ordered set such that**
  - $y_1$  explains highest percentage of variance in resource demands
  - successive  $y_i$  explain increasingly lower percentages

# Sample Problem

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- Given a set of **n** workstations
  - $x_{s_i}$  number of packets sent by workstation i
  - $x_{r_i}$  number of packets received by workstation i
- There is a considerable correlation between  $x_{s_i}$  and  $x_{r_i}$
- Compute  $y_{ki}$   $k=1,2$  for each workstation i, such that successive  $y_k$  vectors provide next best discriminatory power