

Collective Actuation

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DPR & Claytronics Teams

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***Dynamic Physical Rendering**
Intel Research Pittsburgh

#Claytronics
Carnegie Mellon University



Background: Intel Lab at Carnegie Mellon



- Located on the 4th floor of the “Collaborative Innovation Center” (CIC) building

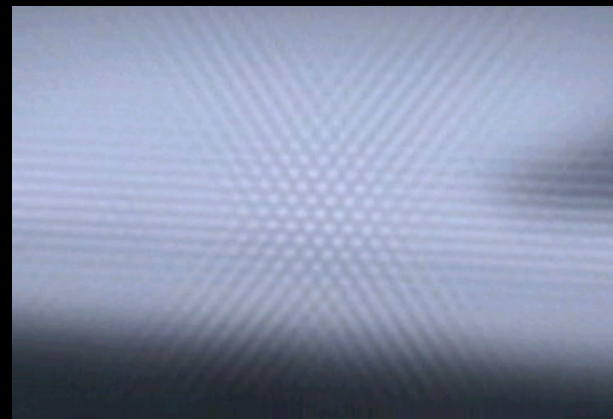
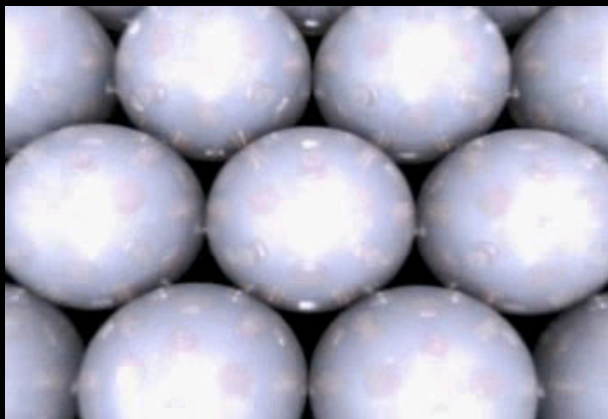
Background: DPR (Intel) & Claytronics (CMU)

- Our focus is on *shape-changing ensembles*
- Envision sub-millimeter modules, used in groups of 10^4 to 10^8 units

Long-term project goals:

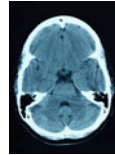
- Scalable software architecture and tools for millions of cooperating agents
- Hardware design (concepts) suitable for integrated photolithographic + self-assembly manufacture





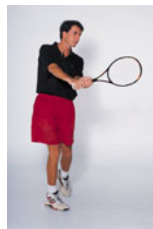
Other Applications

- 3D Visualization & interface
(medical, etc.)



- Product design,
computer-assisted sculpting

- New forms of telepresence-based
human-human communication



- Shape-shifting antennas
- Variable form-factor
computing devices
- Malleable user interfaces
- 3D facsimile sampling
and reproduction

Some Aspects of Shape Control

- Stretchable/shrinkable “lattices”
- Linear actuators, even with spherical modules
- Larger forces than those possible from a pair of modules alone
- ~Millions of cooperating modules
 - Must reduce overall control complexity
 - Need to deal with failures and variability locally
- Likely trade off spatial resolution (module size) vs. increase strength of each module’s actuators

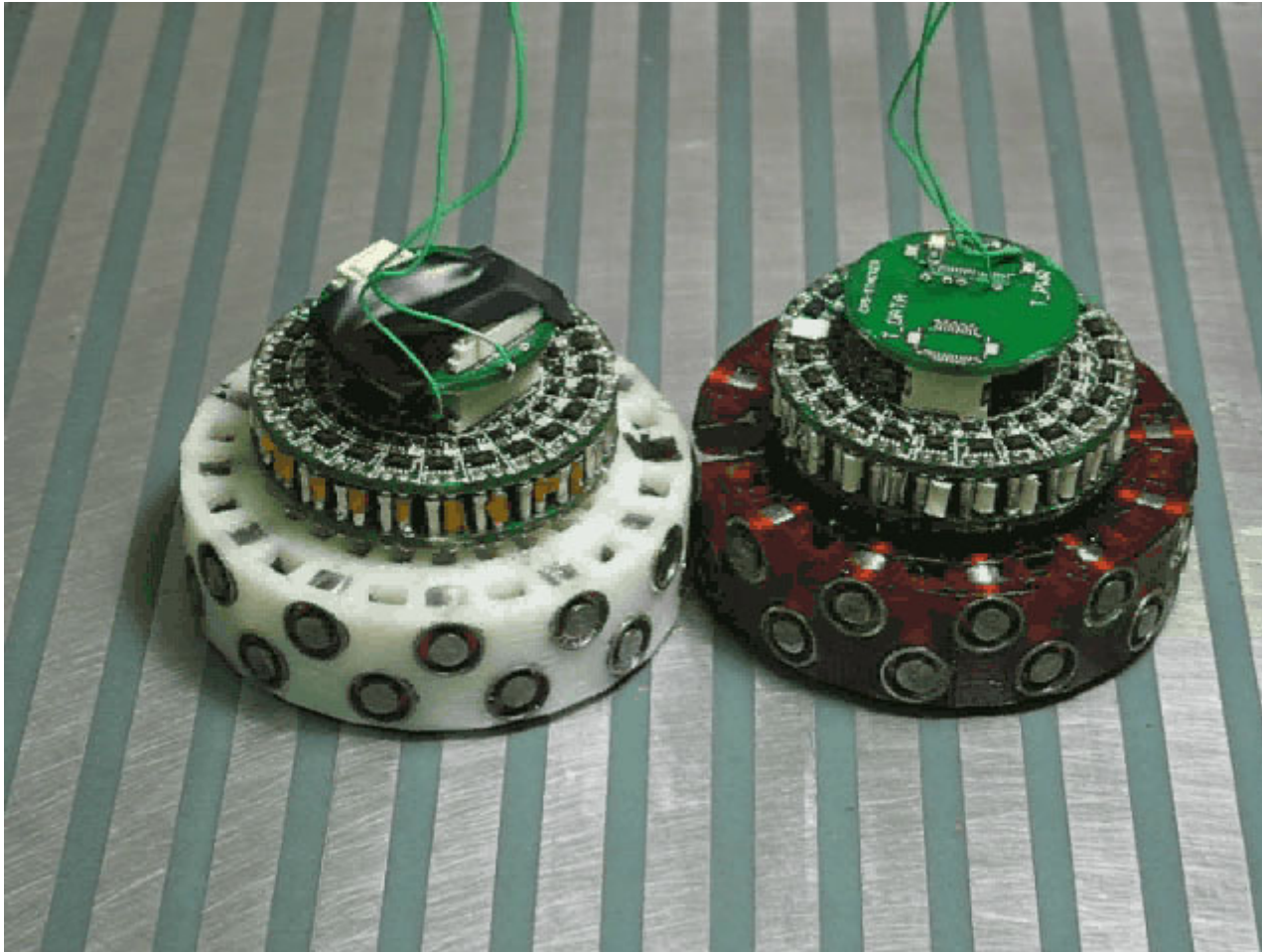


Mesoscale prototype catoms

- Cylindrical (~5cm = 2 inch across)
- Electromagnetic actuators/latches

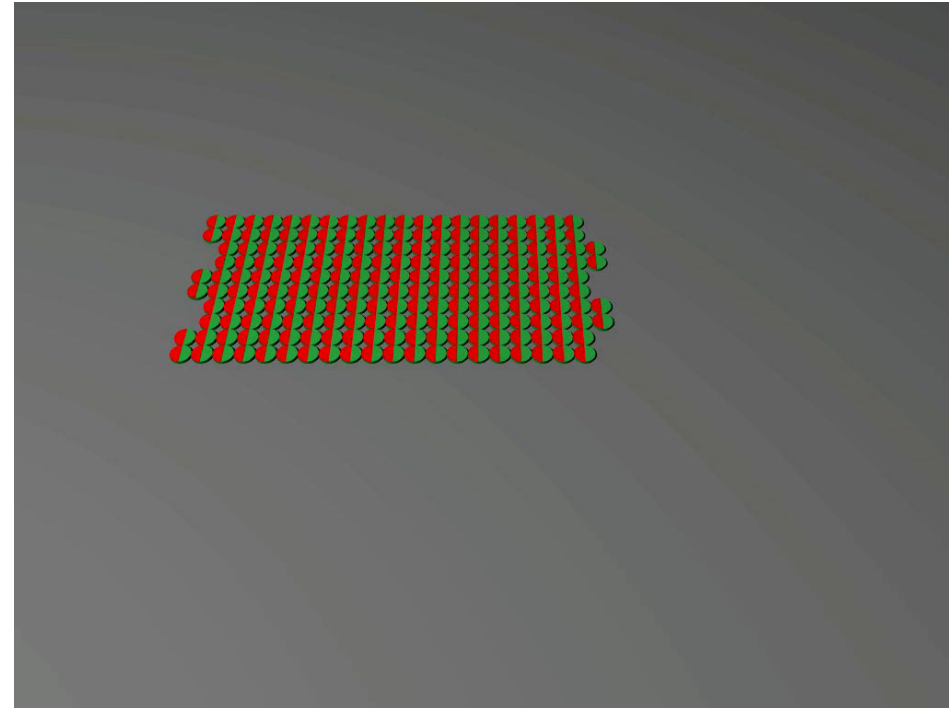
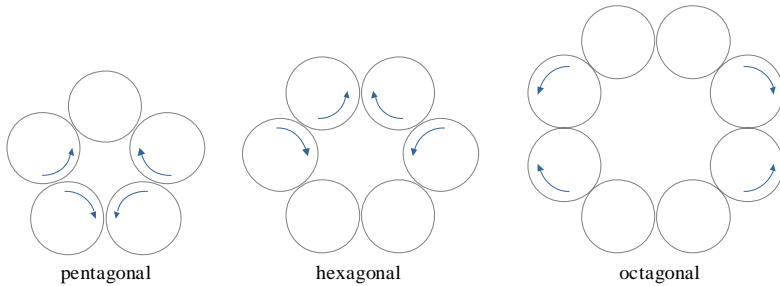


Electromagnetic Rolling Demo



Physical Manipulation Cast as a Software Problem: "Collective Actuation"

*Compose groups of catoms where
the outside dimensions change via internal rolling*



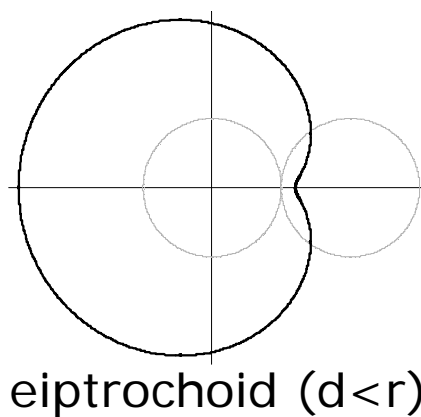
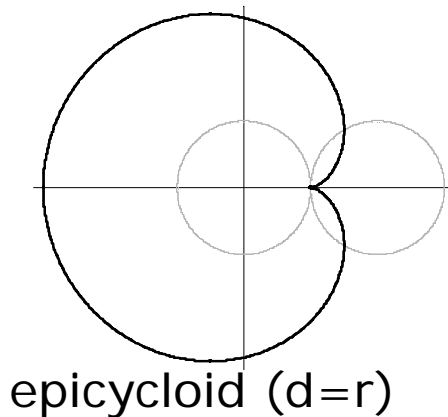
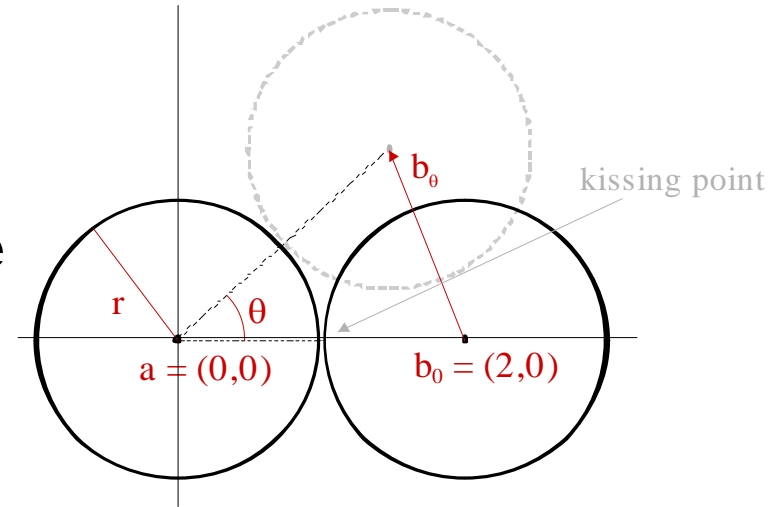
Related Work

- Parallel Manipulators [Luntz97] [Böhringer]
- Atron chains [Christensen06]
- Rolling locomotion for chain-style MRRs [Atron, Polybot, Superbot]

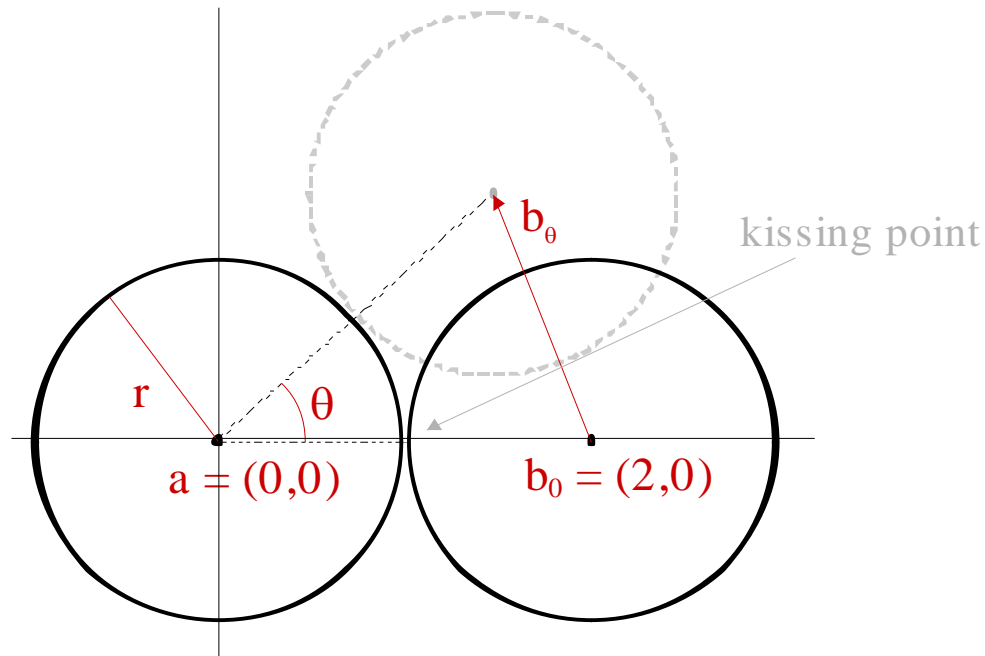


Kinematics of Module Rolling

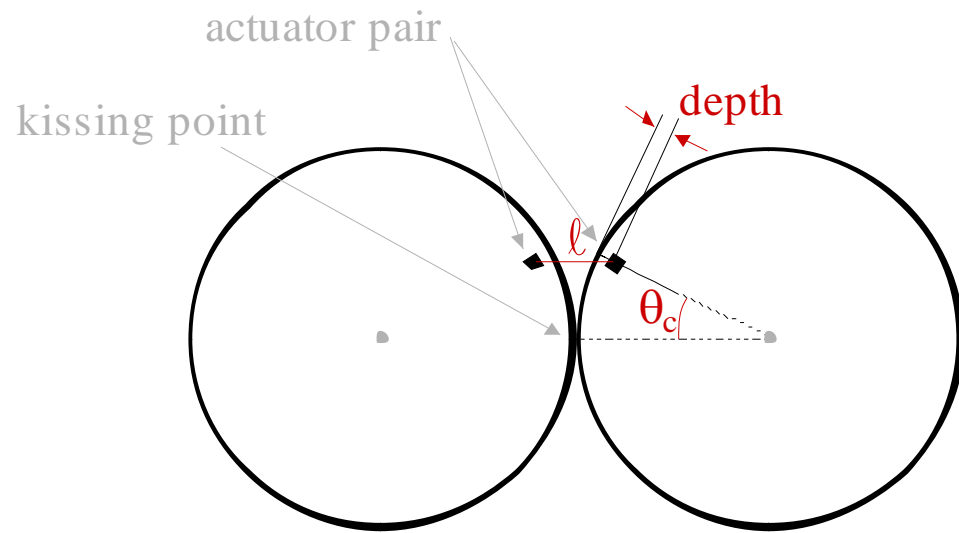
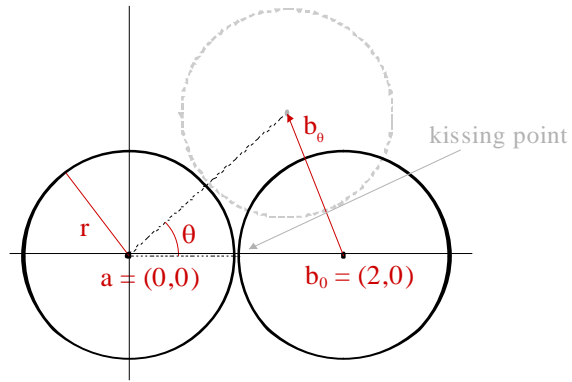
- Treat one module as static, the other as moving
- Center of the moving module traces a circle centered on the static module
- Points outside the center of the moving module trace epitrochoids (or epicycloids for $d=r$)



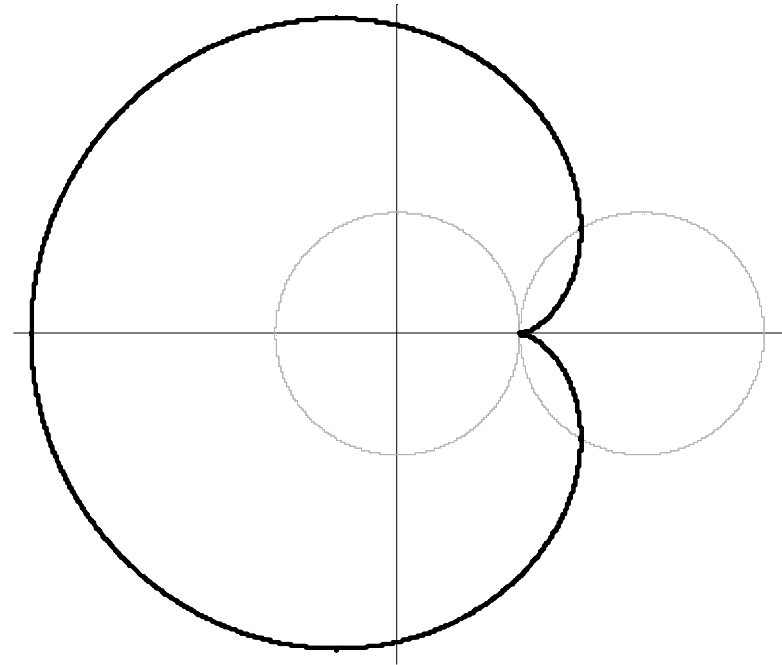
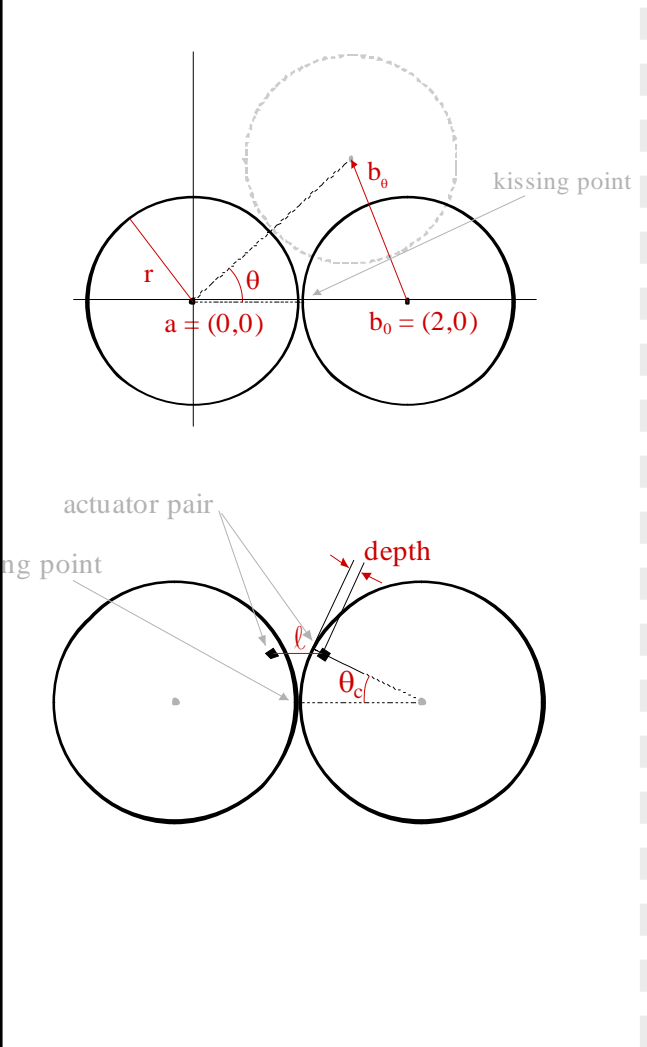
Motion model: Rolling circular modules



Actuator locations

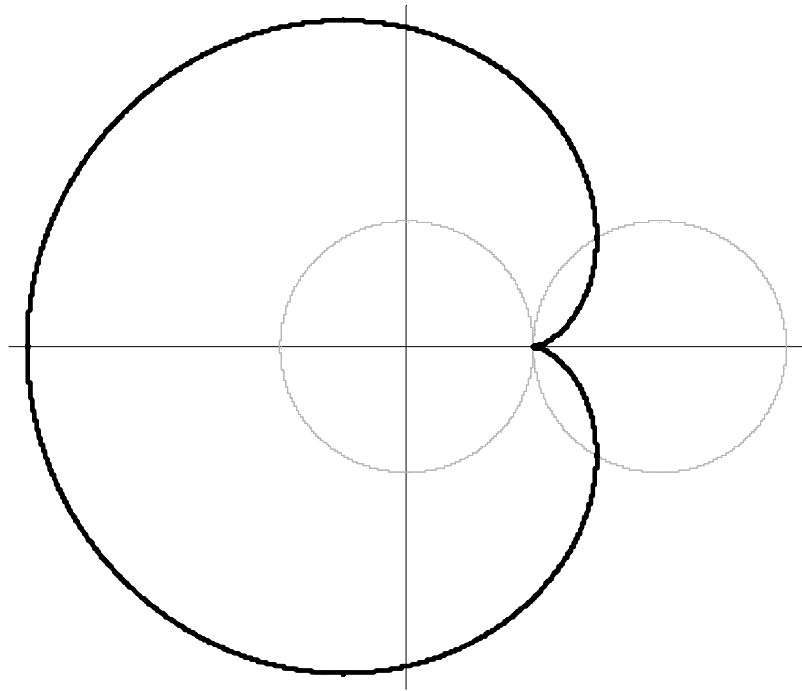


Path of one actuator relative to the other



Epicycloid

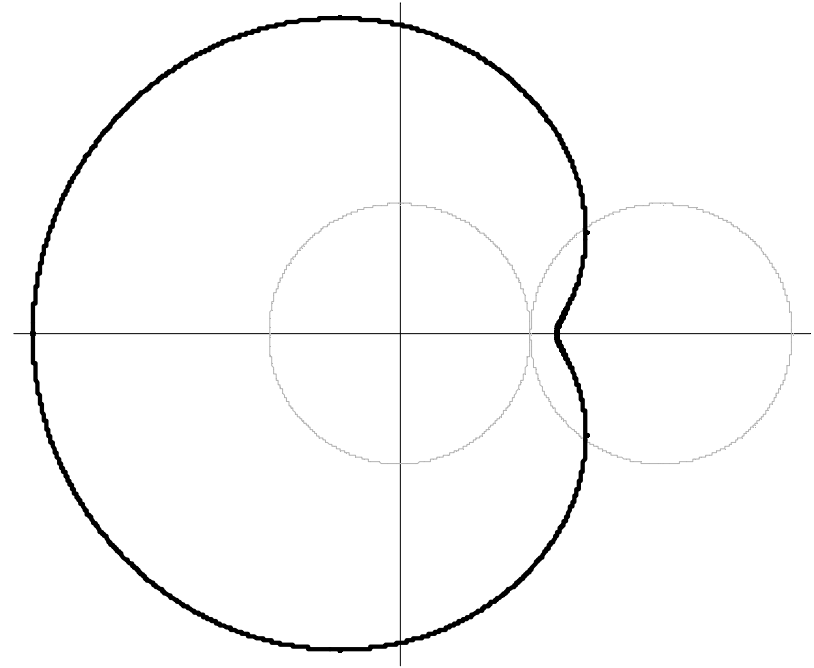
(depth=0)



&

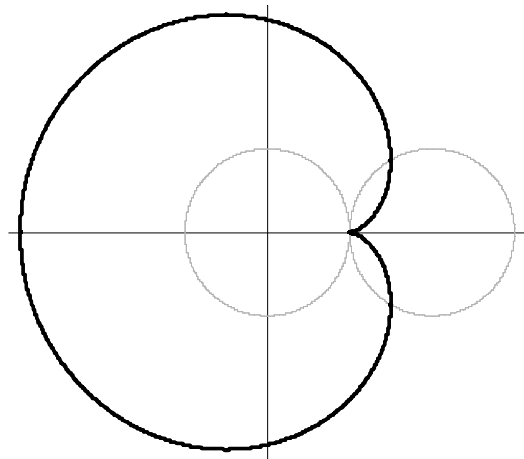
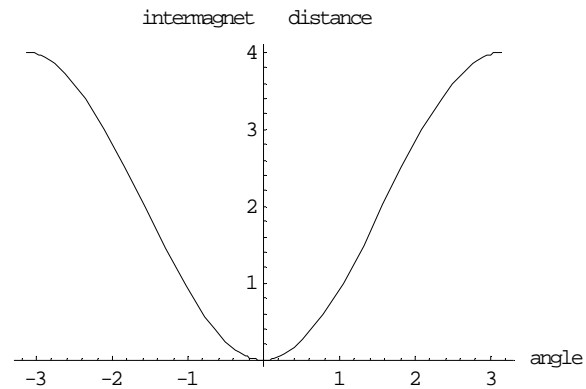
Epitrochoid

(depth>0)



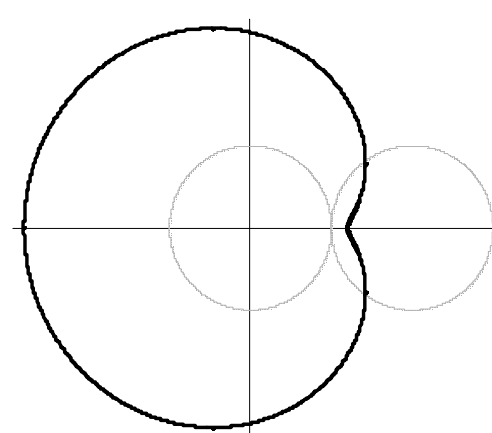
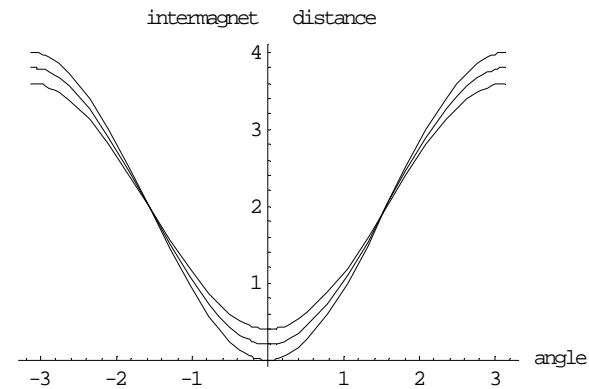
Epicycloid

(act. depth=0)



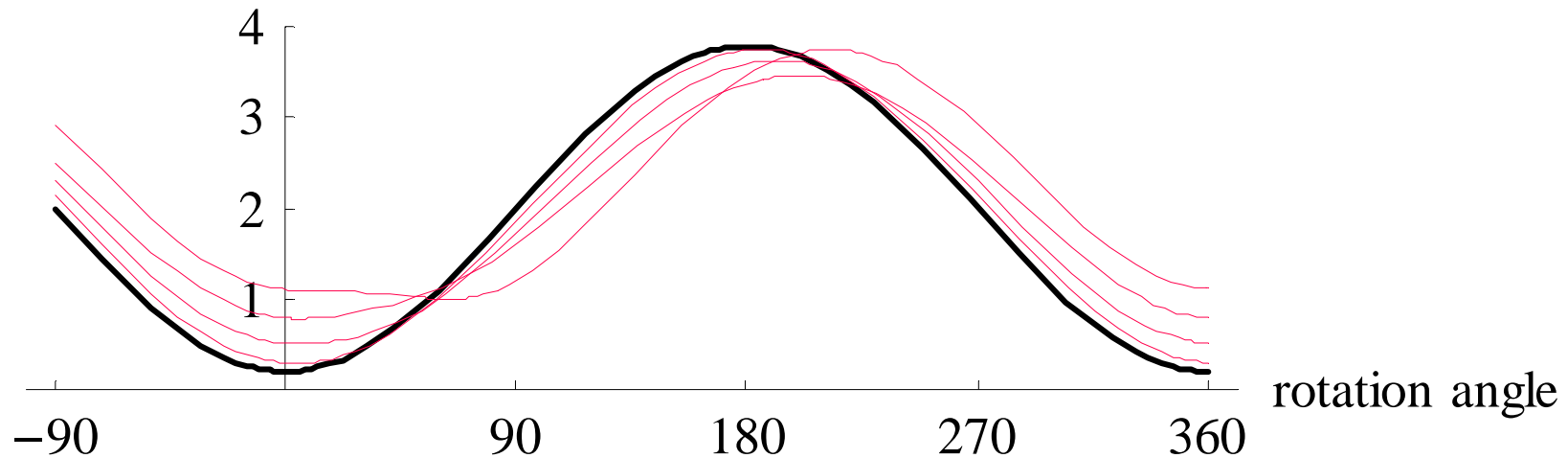
& Epitrochoid

(act. depth>0)

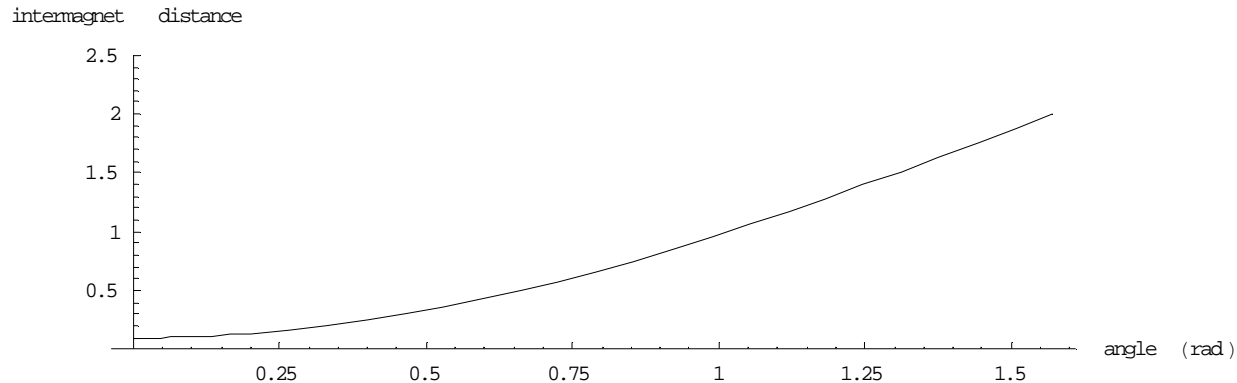


A sinusoidal approximation is close, even for out of phase actuators

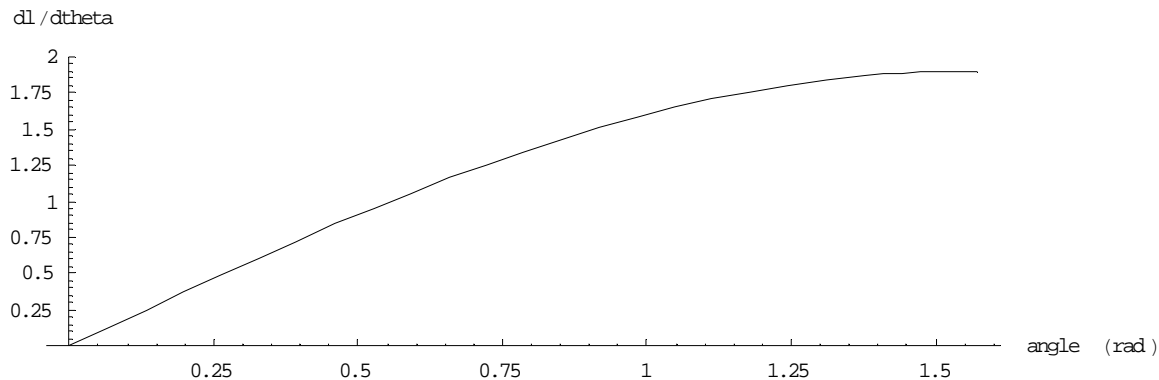
distance between actuators



Based on the intercatom geometries,
we get a varying “lever arm”
(i.e., mechanical advantage)



distance
between
actuators



mechanical
advantage

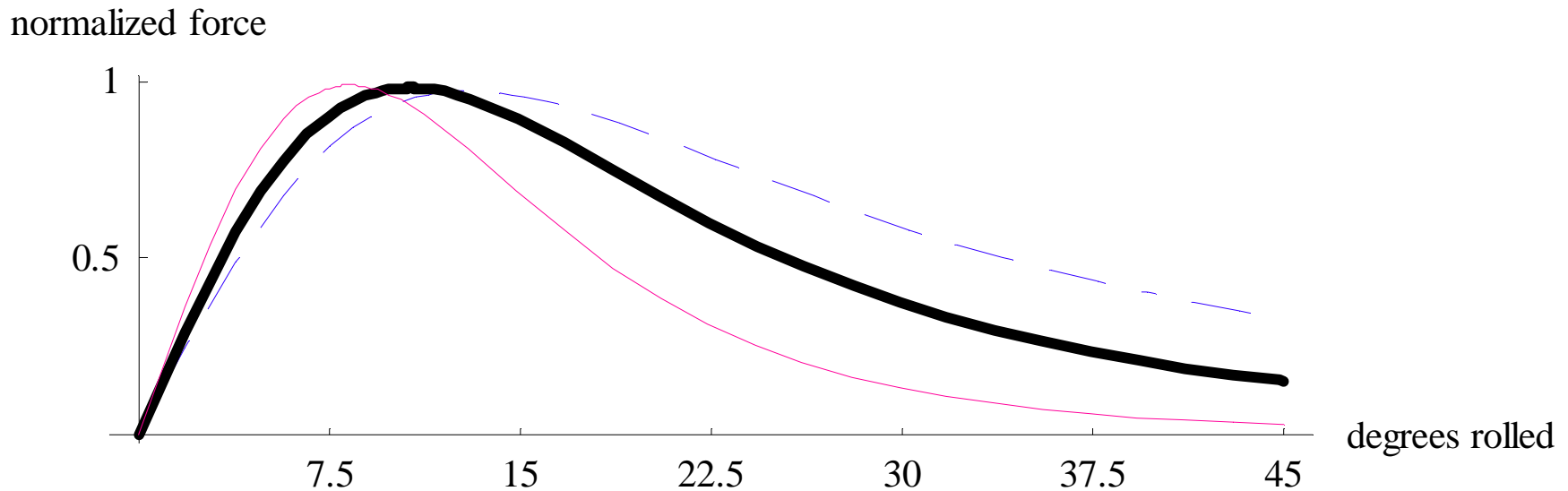
0

angle

180

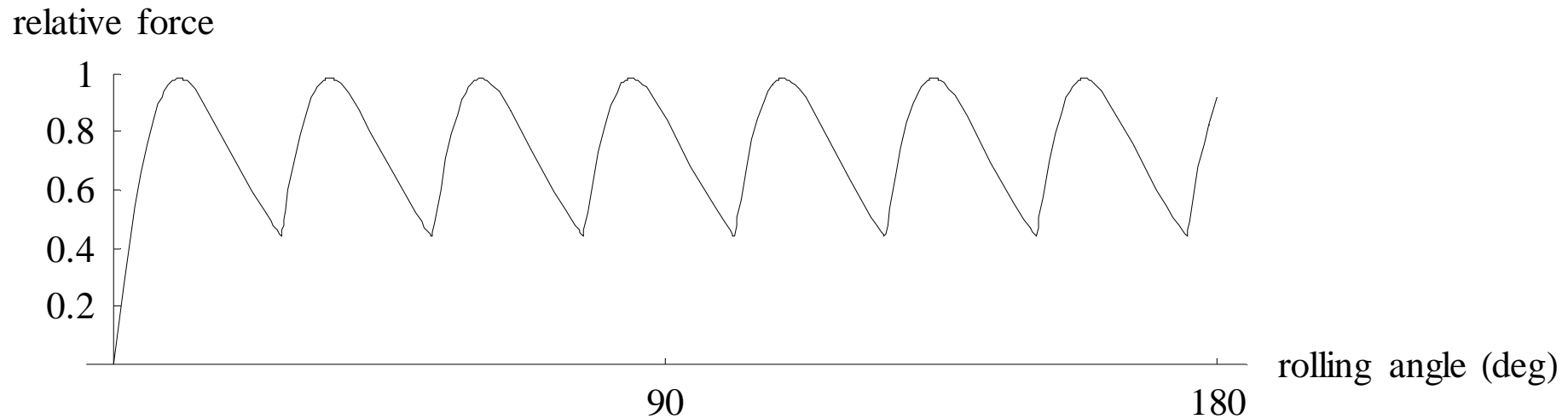


Combining the effects of lever arm and force law (inverse square, etc.)



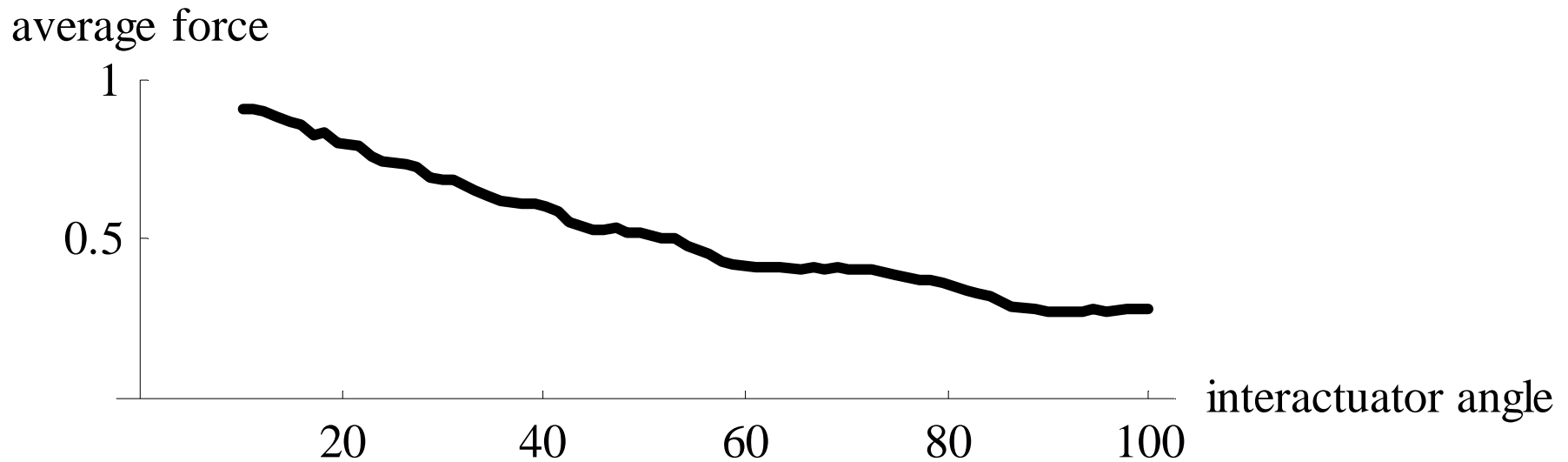
red = inverse cube
black = inverse square
blue = inverse semilog

Composing multiple actuators



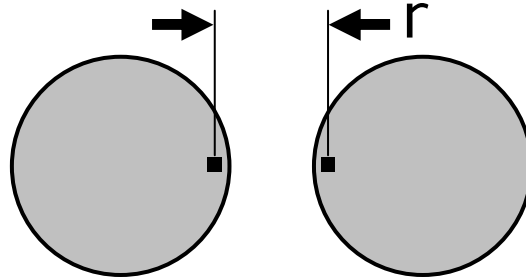
actuator spacing = 25° , $d=5\%$, inverse square law,
only one pair of actuators is active at any given time

mean vs peak force over varying interactor angles



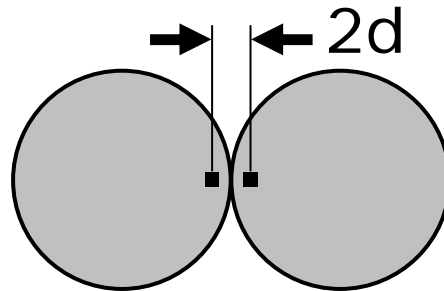
Quantifying actuator force in our unitless analysis

"unit" force



f_m

max force



f_{max}

Math (see the paper for details)

$$\mathbf{b} = \begin{bmatrix} 2r \cos \theta \\ 2r \sin \theta \end{bmatrix} \quad \frac{d\mathbf{b}}{d\theta} = \begin{bmatrix} -2r \sin \theta \\ 2r \cos \theta \end{bmatrix}$$

$$\ell = \begin{bmatrix} (1-d)r - 2r \cos \phi + (1-d)r \cos 2\phi \\ -2r \sin \phi + (1-d)r \sin 2\phi \end{bmatrix} = \begin{bmatrix} -2r(\cos \phi)(1 + (d-1)\cos \phi) \\ -2r(1 + (d-1)\cos \phi) \sin \phi \end{bmatrix}$$

$$|\ell| = 2r + (2rd - 2r) \cos \phi$$

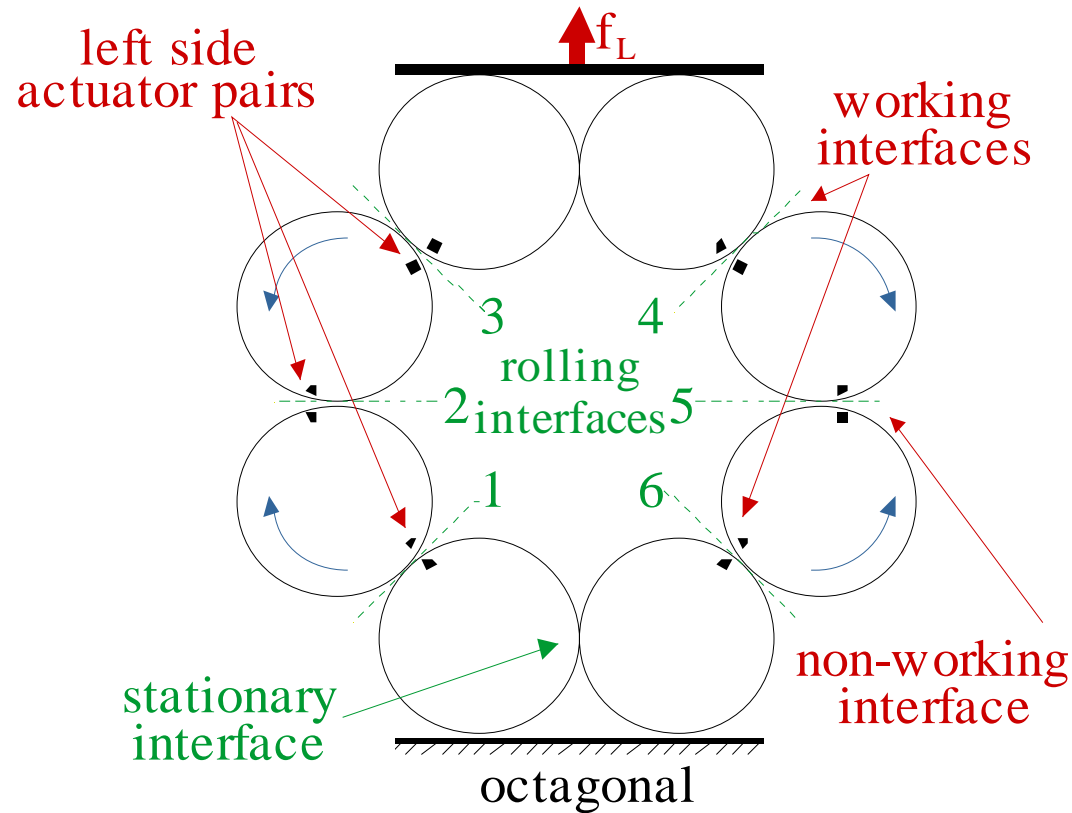
$$\frac{d|\ell|}{d\phi} = 2r(1-d) \sin \phi$$

$$\frac{d\mathbf{b}}{d|\ell|} = \frac{d\mathbf{b}}{d\theta} \cdot \frac{d\theta}{d|\ell|} = \begin{bmatrix} -2r \sin \theta \\ 2r \cos \theta \end{bmatrix} \cdot \frac{1}{2r(1-d) \sin(\theta_c - \theta)} = \frac{\csc(\theta_c - \theta)}{d-1} \begin{bmatrix} \sin \theta \\ -\cos \theta \end{bmatrix}$$

$$q = \frac{d\mathbf{b}}{d|\ell|} \ell^\gamma = \frac{\csc(\theta_c - \theta)(2r - (2r - 2d) \cos(\theta - \theta_c))^\gamma}{d-1} \begin{bmatrix} \sin \theta \\ -\cos \theta \end{bmatrix}$$

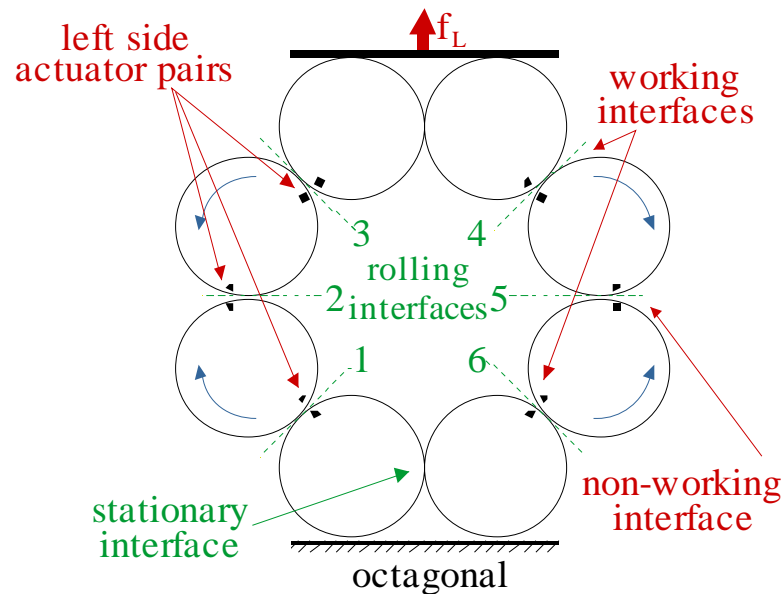
$$f_L = 2 \left(\frac{3}{2} \right) \left(\frac{1}{q \bullet \begin{bmatrix} 0 \\ 1 \end{bmatrix}} \right) f_m = \frac{-3(d-1) \cos \theta}{\csc(\theta_c - \theta)(2r - (2r - 2d) \cos(\theta - \theta_c))^\gamma} f_m$$

Lifting force for an octagonal cell



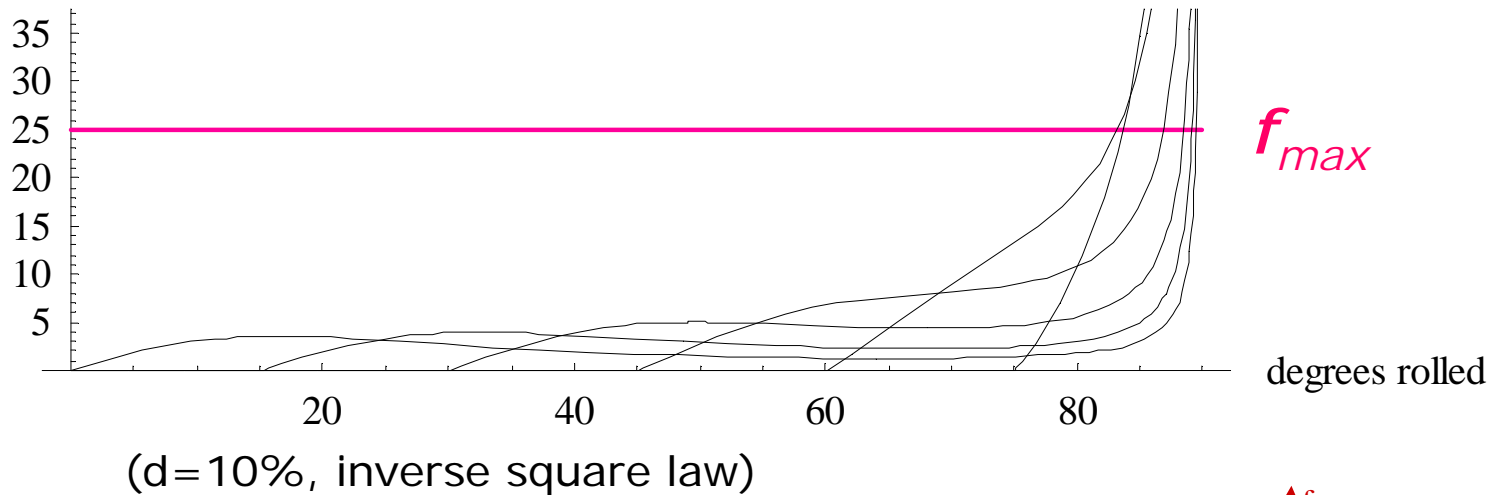
Lifting force for an octagonal cell

$$f_L = 2\left(\frac{3}{2}\right)\left(\frac{1}{q \bullet \begin{bmatrix} 0 \\ 1 \end{bmatrix}}\right) f_m = \frac{-3(d-1)\cos\theta}{\csc(\theta_c - \theta)(2r - (2r - 2d)\cos(\theta - \theta_c))^\gamma} f_m$$

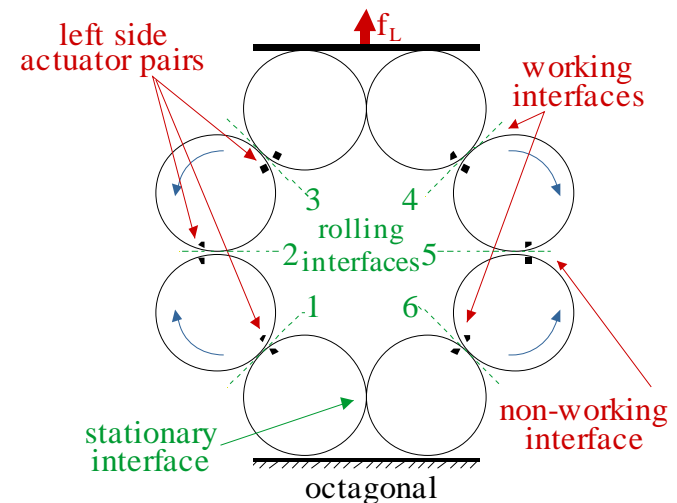


Lifting force for an octagonal cell

lifting force

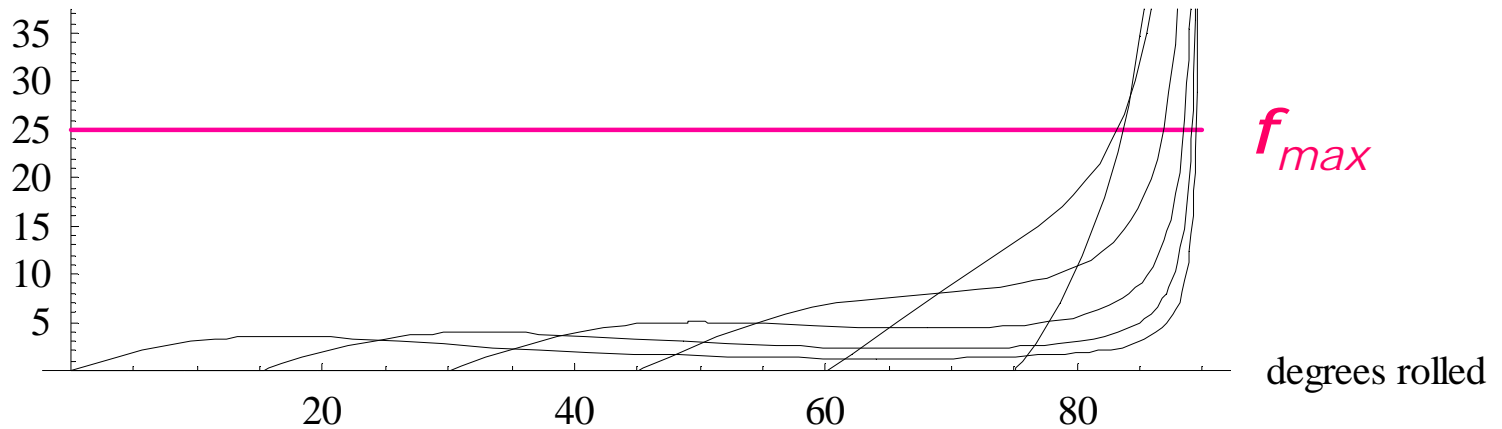


$$f_L = 2 \left(\frac{3}{2} \right) \left(\frac{1}{q \bullet \begin{bmatrix} 0 \\ 1 \end{bmatrix}} \right) f_m = \frac{-3(d-1)\cos\theta}{\csc(\theta_c - \theta)(2r - (2r - 2d)\cos(\theta - \theta_c))^\gamma} f_m$$

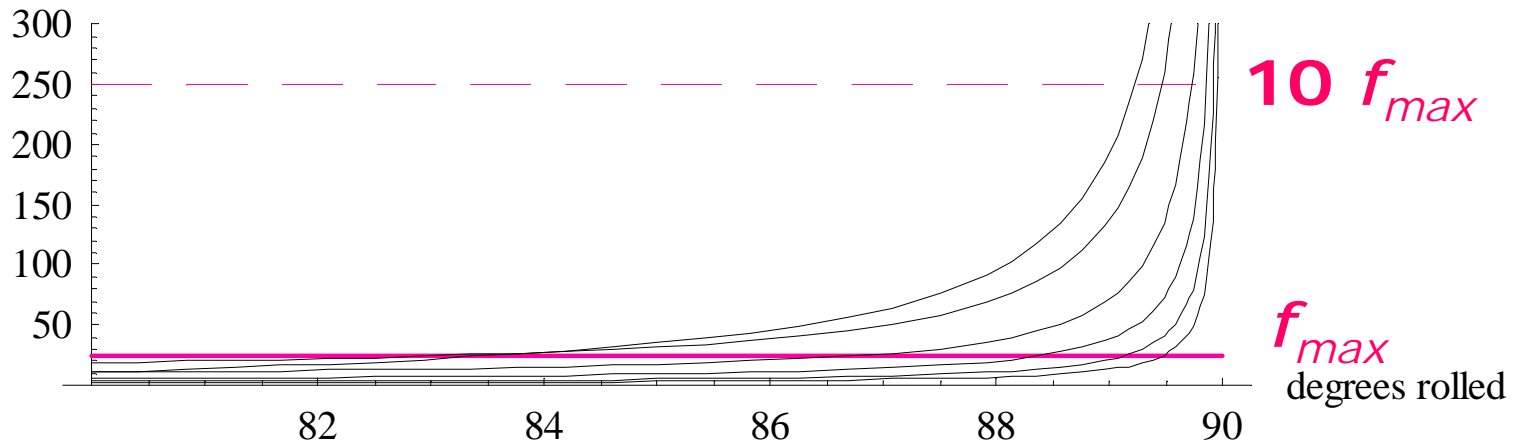


Lifting force for an octagonal cell

lifting force

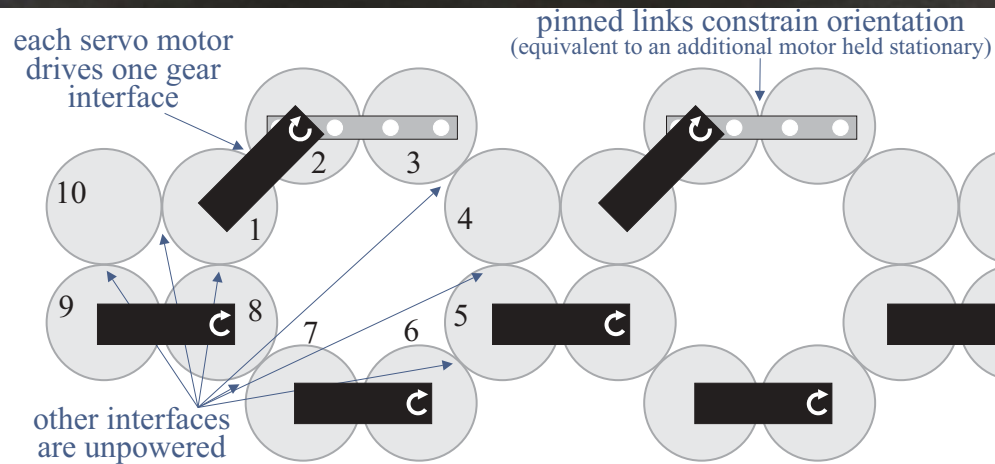
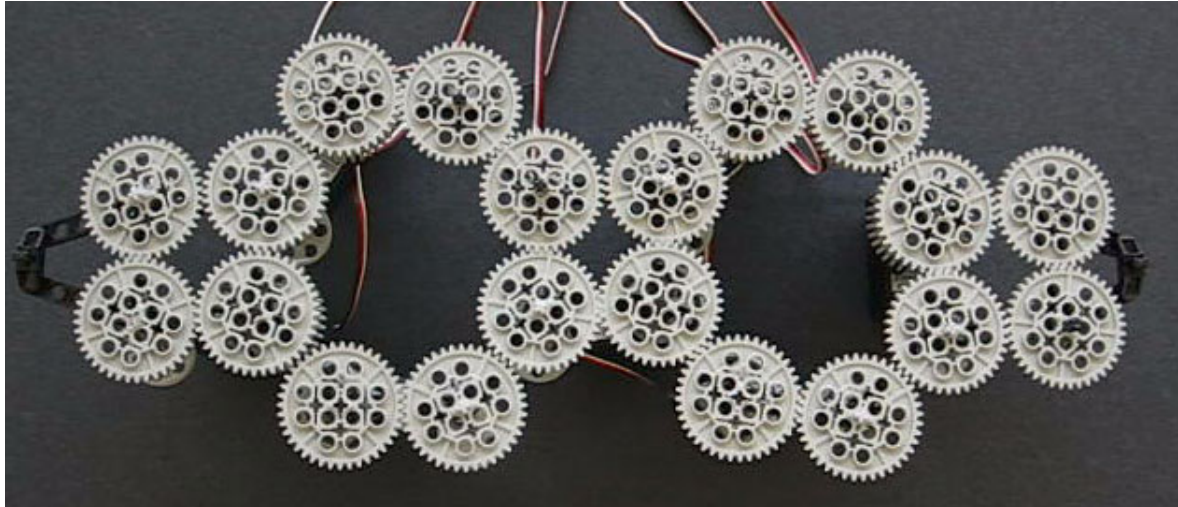


lifting force

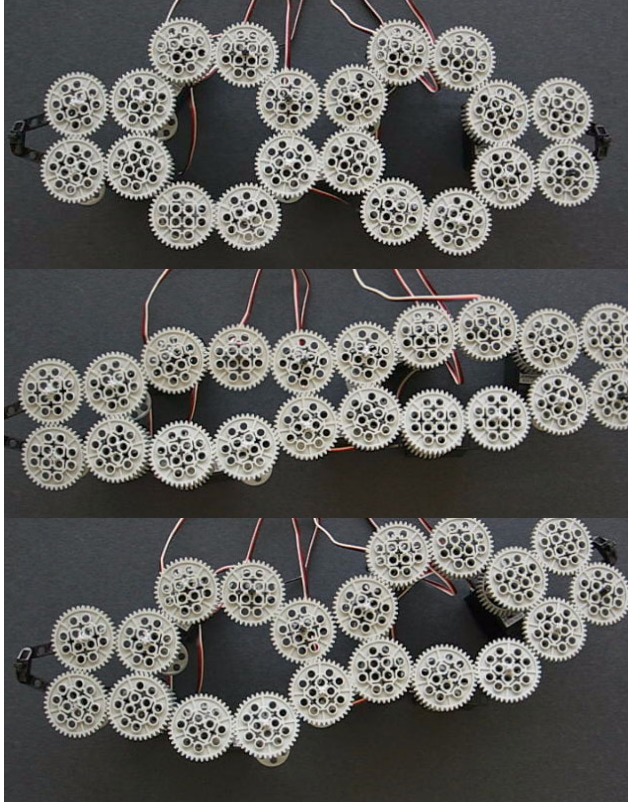


d=10%, inverse square law

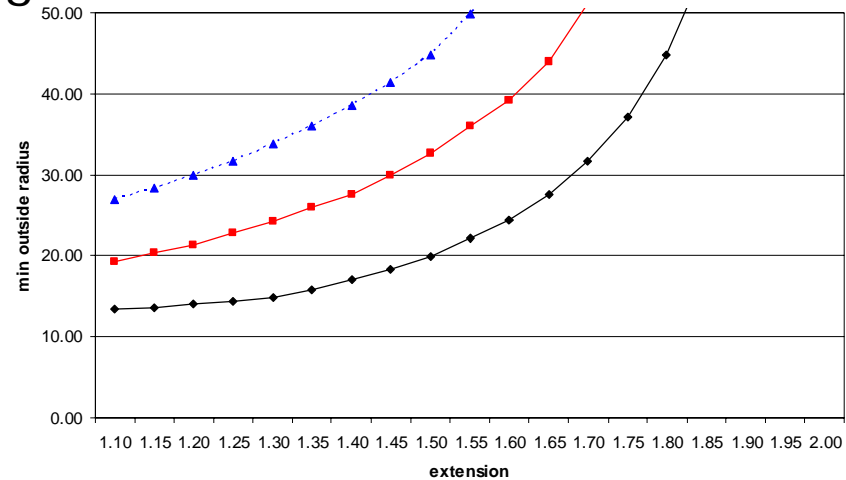
Experiment: Self-Articulating Structures



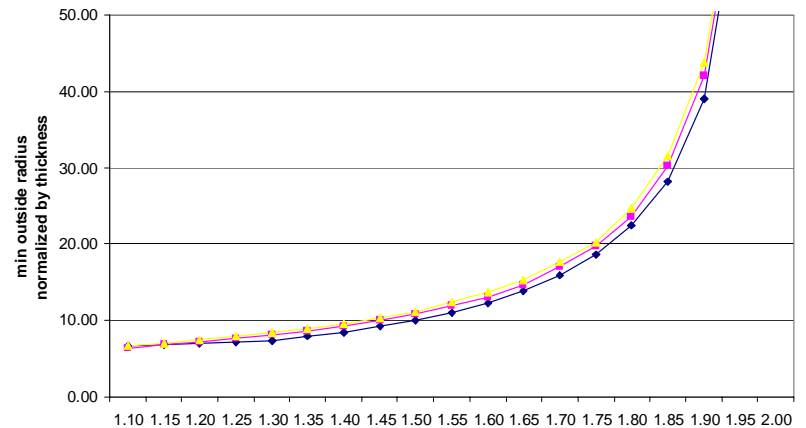
Experiment: Self-Articulating Structures



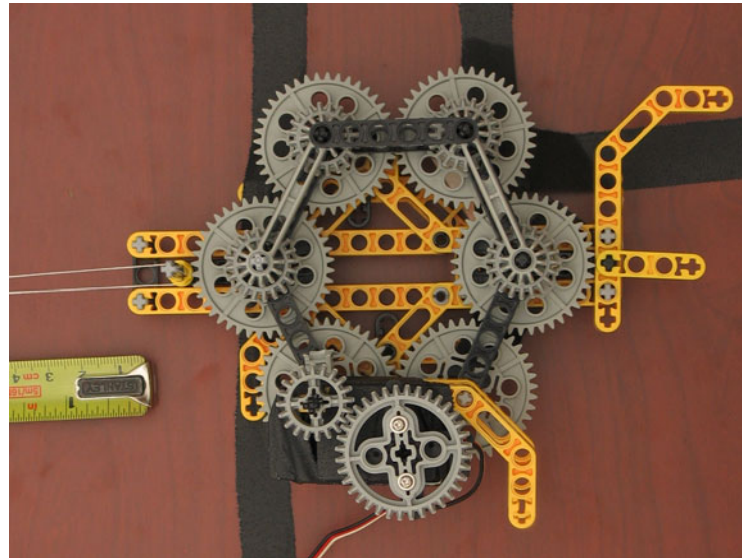
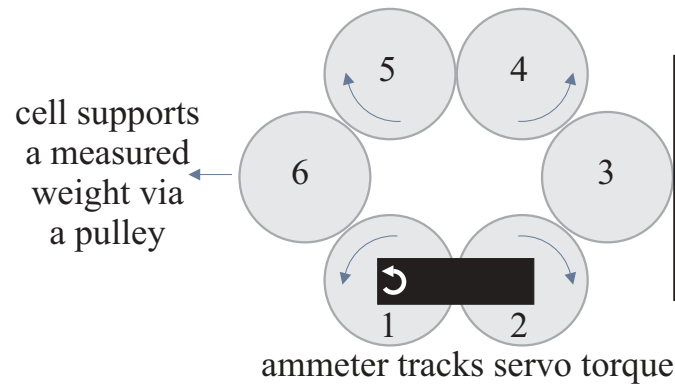
tightest curvature achieved vs extension



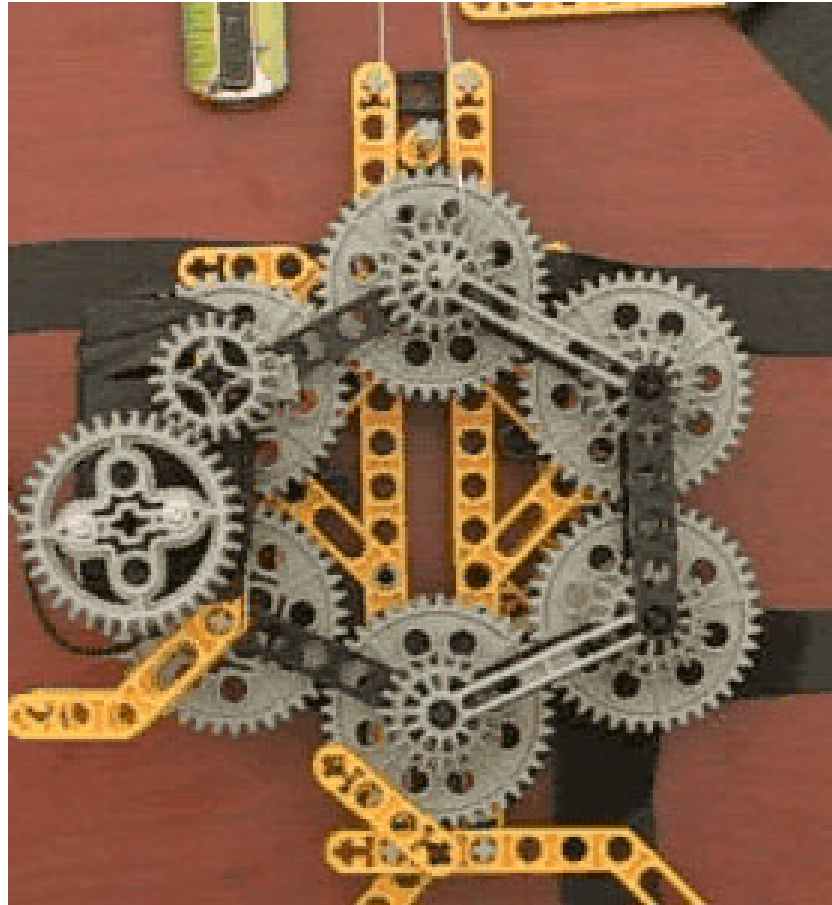
curvature normalized to beam thickness



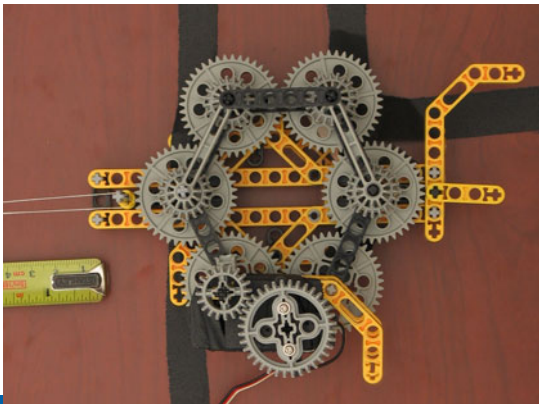
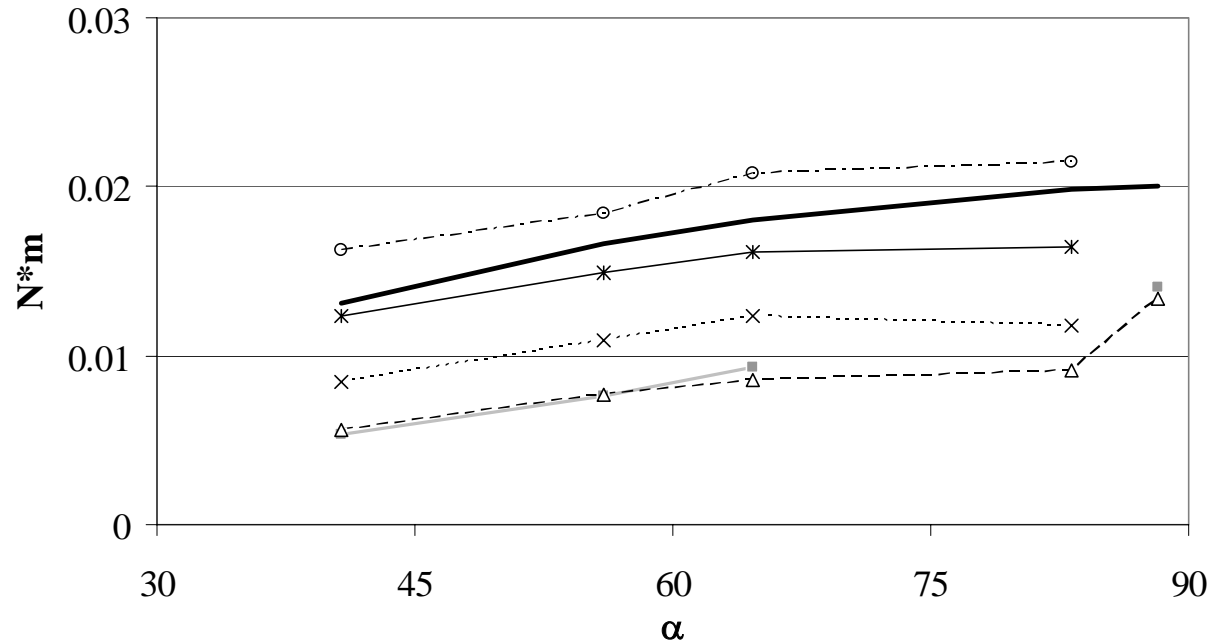
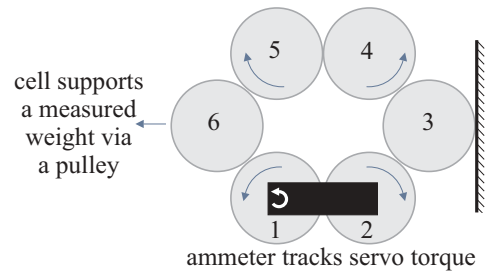
Experiment: Force Test Cell



Experiment: Force Test Cell



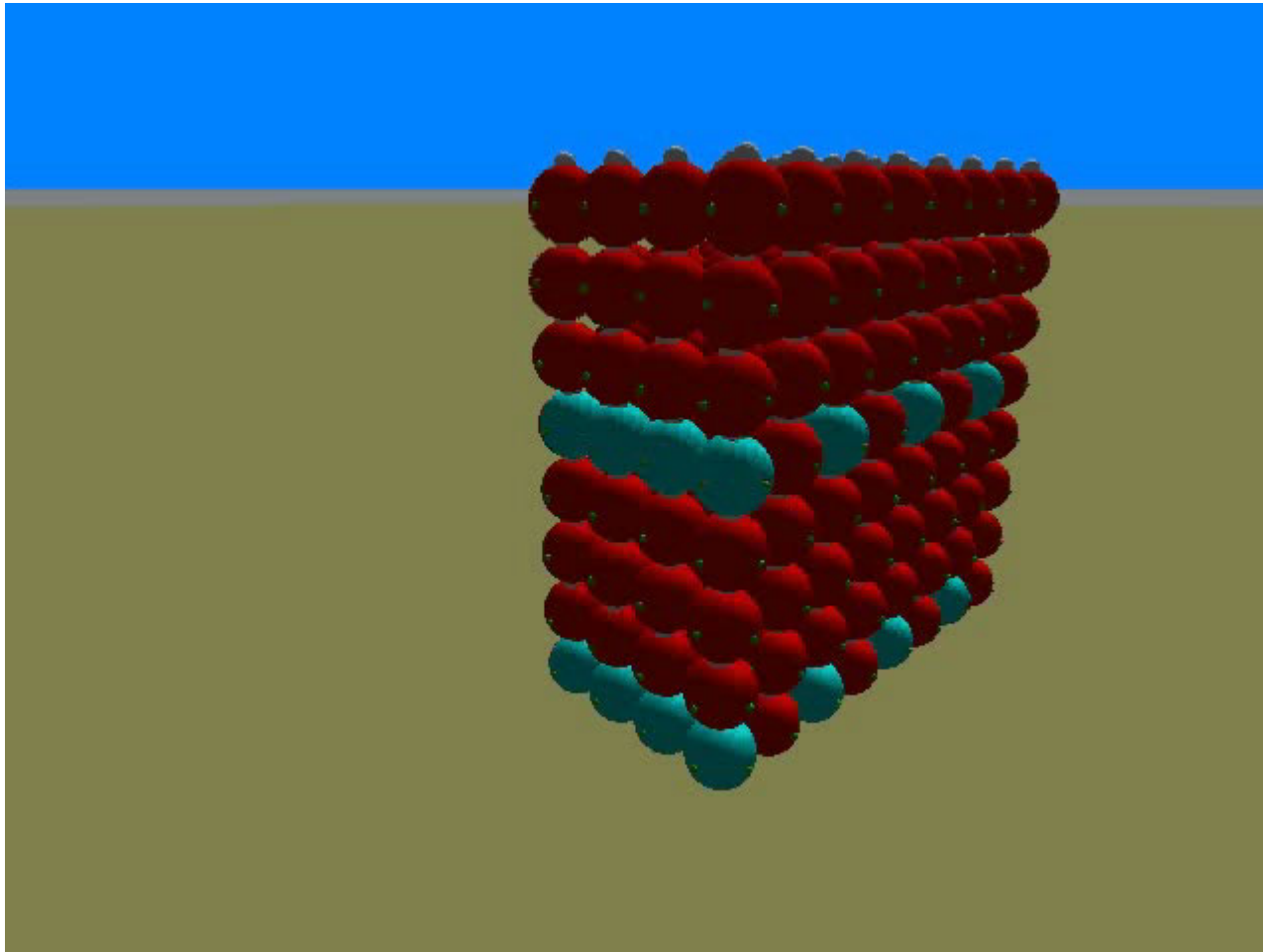
Experiment: Force Test Cell



Pinned gears + Servos



3D Simulation



Control Complexity / Bandwidth Observations

- **Reduced DOF:** Collective Actuation cells offer a reduced degree-of-freedom means of commanding the structure
- **Potential for Aggregation:** Depending upon the shape, adjacent cells may be combined into single logical entities for control purposes
- **Scalability:** Arrays of cells can control large structures with control complexity proportional to the number of desired degrees of freedom in the shape



What works

- **Kinematic Simulation:** octohedral & hexahedral cells in 2D; octohedral in 3D
- **Kinematic Prototypes:** Pinned 2D cells using toothed gears & servos
- **Force-at-distance Driven Prototypes:** Magnetically-retained/driven 2D versions using permanent magnets (illustrate force curves around fixed operating points)



Selected Unsolved Problems

- Stability of rolling modules, particularly in 3D
- Hardware: Robustness of our current force-at-distance actuators is low – so far our electromagnet prototypes don't work sufficiently reliably to test this technique
- Distributed Control Algorithm
(see future work by Ram Ravichandran)
- Dynamics
- Exploit nonuniform failure modes:
It is possible to predict which bonds will break when a cell is overloaded – use this property to strengthen cells or detect and respond to failures



